COMPUTER PROGRAM LISTING APPENDIX



```
Votc.h
* file:
           tc v2.h
 * date:
           April 12, 2000
* function:
           tests turbo codes
           Modulation: QAM
           Decoder: MAP algorithm
          *********************
#include <math.h>
#include <stdio.h>
#include <malloc.h>
#include <dos.h>
/* Definition of the first recursive systematic code (RSC1):
#define RSC1 ENC MEM 4
                        /* encoder memory order
#define RSC1 STATES
               (1 << RSC1_ENC_MEM)
#define RSC1_FP
                           /* forward polynomial in octal
               035
#define RSC1_BP
               023
                           /* backward polynomial in octal
/* Definition of the second recursive systematic code (RSC2):
#define RSC2 ENC MEM 4
                           /* encoder memory order
#define RSC2 STATES
               (1 << RSC2 ENC MEM)
#define RSC2 FP
               035
                          /* forward polynomial in octal
#define RSC2 BP
               023
                           /* backward polynomial in octal
#define NR ITER
                           /* nr. of iterative decoding stages
                           /* Eb/No in dB
               6.0
#define EBNO
#define MAX ERRORS
               1000
                           /* stop when this nr. is reached
#define INT_SIZE
                           /* nr. of info bits to be ileaved
               6144
#define MAX
               (exp(31.0))
                           /* limit soft outputs
#define E STEPS
               1000
                           /* number of values for E val
                           /* how often to print results
#define PRINT_BLOCKS 100
#define SEED1
               13733
                           /* seeds for random nr. gen.
#define SEED2
               1935791
#define SIGMA_12_4AM
                    sqrt(2.50 * pow(10.0, (-EBNO / 10.0))) /* A = 1.0 */
#define SIGMA_12_16QAM
                    sqrt(2.50 * pow(10.0,(-EBNO / 10.0)))
#define SIGMA_34_16QAM
                    sqrt((10.0/6.0) * pow(10.0,(-EBNO / 10.0)))
/* For 8AM, 64QAM, 256QAM, A = 0.5 => A*A = 0.25. Thus, Eav = 5.25*A*A = Eav/4 */
#define SIGMA_56_64QAM sqrt(4.2/4 * pow(10.0,(-EBNO / 10.0)))
                    sqrt(5.25/4 * pow(10.0,(-EBNO / 10.0)))
#define SIGMA_46_64QAM
                    sqrt(5.25/4 * pow(10.0,(-EBNO / 10.0)))
#define SIGMA_23_8AM
                   sqrt(7.0/4 * pow(10.0,(-EBNO / 10.0)))
sqrt(17.0/4 * pow(10.0,(-EBNO / 10.0)))
#define SIGMA_12_8AM
/* For 4QAM (A = 0.5):*/
/* For 8QAM (A = 0.5):*/
#define SIGMA_36_64QAM sqrt(42.0/6.0/4 * pow(10.0,(-EBNO / 10.0))) /* 3 info */
/* For 16QAM, 64QAM, 256QAM, 1024QAM (A = 0.5):*/
```



```
/* For 32QAM, 128QAM, 512QAM, (A = 0.5):*/
#define SIGMA 8AM of 721 128QAM
                                 sqrt(21.0/2/4 * pow(10.0,(-EBNO / 10.0))) /* 1 info */
#define SIGMA_32AM_of_39_512QAM
                                sqrt(341.0/4/4*pow(10.0,(-EBNO / 10.0))) /* 2 info */
#define SIGMA 16AM of 39 512QAM
                                sqrt(85.00/2/4*pow(10.0,(-EBNO / 10.0))) /* 1 info */
/* For 32QAM (A = 0.5):*/
                           sqrt(26.0/6/4 * pow(10.0,(-EBNO / 10.0))) /* 3 info */
sqrt(26.0/6/4 * pow(10.0,(-EBNO / 10.0))) /* 3 info */
#define SIGMA_8AM_of_32QAM
#define SIGMA 4AM of 32QAM
/* For R57_128QAM (A = 0.5):*/
#define SIGMA 16AM of 128QAM
                             sqrt(106.0/10/4 * pow(10.0,(-EBNO / 10.0))) /* 3 info */
                             sqrt(106.0/10/4 * pow(10.0, (-EBNO / 10.0))) /* 2 info */
#define SIGMA_8AM_of_128QAM
/* For R69 512QAM (A = 0.5):*/
#define SIGMA 32AM of 512QAM
                             sqrt(426.0/12/4*pow(10.0,(-EBNO / 10.0))) /* 4 info */
#define SIGMA_16AM_of_512QAM
                             sqrt(426.0/12/4*pow(10.0,(-EBNO / 10.0))) /* 2 info */
/* For R710_1024QAM (A = 0.5):*/
#define SIGMA 710 1024QAM sqrt((341.0/7)/4 * pow(10.0,(-EBNO / 10.0))) /* 3.5 info */
/* Define the particular coding and modulation case for simulation
#define R36_64QAM
#define BIT HIST
#define THRESHOLD ITER
                           10
                                    /* record bit histogram for higher iterations */
#define MAX BIT HIST ARRAY
                           (2 * INT SIZE)
                           "../results/R36_64QAM_6144_test_30.err"
#define ERROR FILE NAME
#define FRAME_HIST_FILE NAME "../results/test.fhist"
                           "../results/map.hist"
#define BIT HIST FILE NAME
                           "../results/6144/s6144"
#define INTERLEAVER FILE
 * Notel:
Make sure that for each simulation, the INT SIZE represents the size of the interleaver
defined in INTERLEAVER FILE
 */
* Note2:
In rate 4/6 64QAM TTCM only two bits out of four are coded rate half. Therefore,
the first half of the interleaver table used has a INT_SIZE/2 interleaver,
the rest is mapping the bits in the same position.
 */
```



Votc.c

```
* file:
                 tc_v2.c
 * date:
                 March 20, 2000
 * function:
                 tests turbo codes
                 Modulation: QAM
                 Decoder:
                             MAP algorithm
#include "tc_v2.h"
typedef struct {
  int
               enc state;
                                         /* encoder state
                                         /* number of encoder states
  int
               nr states:
                                         /* encoder memory
  int
               enc mem;
  int
               bp;
                                         /* backward polynomial
  int
                                         /* forward polynomial
               fp;
                                        /* previous state for i=0 branch
  int
               *POstate;
  int
               *P1state;
                                        /* previous state for i=1 branch
  int
               *NOstate;
                                        /* next state for i=0 branch
                                        /* next state for i=1 branch
  int
               *N1state;
  int
               *Coded0;
                                         /* coded bit for i=0 branch
  int
               *Coded1;
                                         /* coded bit for i=1 branch
} jat_code;
               jat_map1(jat_code *, double *, double *, double *);
jat_map2(jat_code *, double *, double *, double *);
void
void
void
               jat_trellis_bp_fp(jat_code *);
int
               jat_ps(jat_code *, int);
int
               jat_enc_bp_fp(jat_code *, int);
               r_ileav(double *, int *);
r_ileava(int *, int *);
void
void
void
               r_deileav(double *, int *);
void
               r_deileava(int *, int *);
double
               nrgen();
int
               nrgenbin();
double
               gasdev();
int
               errors(int *, double *, int, int);
int
               print_err(int *, double *, int, int, int *);
double
               find tx I(int);
double
               find_tx_Q(int);
int
               *frame hist;
                                         /* how many frames with how many errors*/
               **bit_hist_array;
                                         /* pointer to NR_ITER pointers
int
                                         to blocks of data organised as:
                                               block nr., bit pos. in error,
                                                block nr., bit pos. in error
int
               *bit_hist block;
                                         /* current number of blocks in error
                                         for each iteration
int
               frame err;
                                         /* frame/block error rate
                                        /* total nr. of err. after NR_ITER
int
               total err;
                                        /* seed generators
long
               s1, s2;
main()
jat_code
               *jat_code1;
jat code
               *jat code2;
int
               u1, u2, u3, u4, u5, u6;
                                         /* bits of a 64QAM symbol in TTCM
              tx_I, tx_Q, rx_I, rx_Q;
v00_I, v00_Q, v01_I, v01_Q, v10_I, v10_Q, v11_I, v11_Q;
double
double
int
               i, j, k, block, iteration;
int
               *rule
                                  /* interleaver
                                   /* the information block of data
int
               *data:
```

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int
               *data_i;
                                   /* the interleaved information block of data*/
                                   /* the deinterleaved inf. block of data
int
               *data d;
                                   /* Encoder1 output
int
               *Encl;
               *Enc2;
                                   /* Encoder2 output
int
                                   /* stores nr. err. for each iteration
               *no_err;
int
               *D1_data;
                                   /* Decoderl input data
double
double
               *D1_parity;
                                   /* Decoder1 input parity
                                   /* Decoder1 input a priori information
              *D1_app;
double
               *D1 exi;
                                   /* Decoder1 output extrinsic information
                                                                                  */
*/
*/
double
                                   /* Decoder2 input data
              *D2_data;
double
              *D2_parity;
*D2_app;
                                   /* Decoder2 input parity
double
                                   /\star Decoder2 input a priori information
double
double
              *D2_exi;
                                   /* Decoder2 output extrinsic information
                                   /* Decoded data
double
               *Dec_data;
double
               *Zero data;
                                   /* zero data
double
              d0, d1, d2, d3, d4, L_d0, L_d1, L_d2, L_d3, tx, rx, K, noise1, n;
double
              L_d4, L_d5;
              L_u1, L_u2, L_u3, L_u4, L_u5, L_u6;
double
double
              noise_I, noise_Q;
FILE
               *out file = NULL;
s1
          = SEED1; /* initialize the seeds for the noise generator
          = SEED2;
frame_err = 0;
total err = 0;
 * initialize the code structures:
jat codel
                      = (jat_code *)malloc(sizeof(jat_code));
                     = RSC1_ENC_MEM;
jat_code1->enc_mem
jat_code1->bp
                      = RSC1_BP;
jat code1->fp
                      = RSC1_FP;
jat code1->enc state = 0;
jat_codel->nr_states = (1 << RSC1_ENC_MEM);</pre>
jat_code1->POstate = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat code1->P1state
                    = (int *)malloc(sizeof(int)*jat code1->nr states);
jat_code1->N0state
                     = (int *)malloc(sizeof(int)*jat_code1->nr_states);
                     = (int *)malloc(sizeof(int)*jat_codel->nr_states);
= (int *)malloc(sizeof(int)*jat_codel->nr_states);
jat codel->N1state
jat code1->Coded0
jat_code1->Coded1
                      = (int *)malloc(sizeof(int)*jat_codel->nr_states);
jat_trellis_bp_fp(jat_code1);
                      = (jat_code *)malloc(sizeof(jat code));
jat code2
                      = RSC2_ENC_MEM;
jat_code2->enc_mem
jat_code2->bp
                      = RSC2_BP;
jat_code2->fp
                      = RSC2_FP;
jat code2->enc state = 0;
jat_code2->nr states = (1 << RSC2 ENC MEM);</pre>
jat_code2->POstate = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_code2->Plstate = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat code2->NOstate = (int *)malloc(sizeof(int)*jat code2->nr states);
jat_code2->N1state
                     = (int *)malloc(sizeof(int)*jat_code2->nr_states);
                      = (int *)malloc(sizeof(int)*jat_code2->nr_states);
= (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat code2->Coded0
jat code2->Coded1
jat_trellis_bp_fp(jat_code2);
data = (int *)malloc(sizeof(int) * INT_SIZE);
if(data == 0)
    printf("Couldn't allocate data memory!\n");
    exit(1);
data i = (int *)malloc(sizeof(int) * INT SIZE);
if(data_i == 0)
    printf("Couldn't allocate data_i memory!\n");
    exit(1);
```



```
data_d = (int *)malloc(sizeof(int) * INT_SIZE);
if(data_d == 0)
  {
    printf("Couldn't allocate data d memory!\n");
    exit(1);
no_err = (int *)malloc(sizeof(int) * NR_ITER);
if(no err == 0)
    printf("Couldn't allocate no err memory!\n");
    exit(1);
else
  for(i = 0; i < NR_ITER; i++)
    no_err[i] = 0;
Enc1 = (int *)malloc(sizeof(int) * INT SIZE);
if(Enc1 == 0)
    printf("Couldn't allocate Enc1 memory!\n");
    exit(1);
Enc2 = (int *)malloc(sizeof(int) * INT SIZE);
if(Enc2 == 0)
    printf("Couldn't allocate Enc2 memory!\n");
    exit(1);
  }
D1_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1 data == 0)
    printf("Couldn't allocate D1 data memory!\n");
    exit(1);
  }
D1_parity = (double *)malloc(sizeof(double) * INT SIZE);
if(D1 parity == 0)
    printf("Couldn't allocate D1 parity memory!\n");
    exit(1);
  }
D1_app = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1 app == 0)
    printf("Couldn't allocate D1 app memory!\n");
    exit(1);
  }
D1_exi = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1_exi == 0)
    printf("Couldn't allocate D1 exi memory!\n");
    exit(1);
 1
D2_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(D2 data == 0)
   printf("Couldn't allocate D2 data memory!\n");
    exit(1);
 }
D2_parity = (double *)malloc(sizeof(double) * INT SIZE);
if(D2_parity == 0)
   printf("Couldn't allocate D2 parity memory!\n");
   exit(1);
```



```
}
D2 app = (double *)malloc(sizeof(double) * INT SIZE);
if(D2 app == 0)
  {
   printf("Couldn't allocate D2 app memory!\n");
    exit(1);
D2_exi = (double *)malloc(sizeof(double) * INT_SIZE);
if(D2 exi == 0)
  {
   printf("Couldn't allocate D2 exi memory!\n");
    exit(1);
Dec_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(Dec data == 0)
    printf("Couldn't allocate Dec data memory!\n");
    exit(1);
Zero_data = (double *)malloc(sizeof(double) * INT SIZE);
if(Zero data == 0)
    printf("Couldn't allocate Zero_data memory!\n");
    exit(1);
for(i = 0; i < INT SIZE; i++)
  Zero_data[i] = 0.0;
frame_hist = (int *)malloc(sizeof(int) * (INT_SIZE+1) * NR ITER);
if(frame_hist == 0)
 {
    printf("Couldn't allocate frame_hist memory!\n");
    exit(1);
 }
else
  {
    for (i = 0; i < (INT SIZE+1)*NR ITER; i++)
      frame_hist[i] = 0;
bit_hist_array = (int **)malloc(sizeof(int *) * 2 * NR ITER);
if(bit hist array == 0)
 {
    printf("Couldn't allocate bit_hist_array memory!\n");
    exit(1);
else
    for(i = THRESHOLD_ITER; i <= NR_ITER; i++)</pre>
       bit_hist_array[i] = (int *)malloc(sizeof(int) * MAX_BIT_HIST_ARRAY);
       bit_hist_array[i+NR_ITER] = bit hist array[i]; /* store the original pointer */
       if(bit_hist_array[i] == 0)
           printf("Couldn't allocate bit_hist_array[i] memory!\n");
           exit(1);
      }
  }
bit_hist_block = (int *)malloc(sizeof(int) * (NR ITER+1));
if(bit_hist_block == 0)
    printf("Couldn't allocate bit_hist_block memory!\n");
    exit(1);
else
```



```
{
    for(i = 0; i <= NR ITER; i++)
      bit_hist_block[i] = 1;
rule = (int *)malloc(sizeof(int) * INT SIZE * 2);
if(rule == 0)
    printf("Couldn't allocate rule memory!\n");
    exit(1);
for(i = 0; i < INT_SIZE; i++)</pre>
 rule[2*i] = 0;
 * read the interleaver file
out_file = fopen(INTERLEAVER FILE, "r");
if(!out_file)
  {
    printf("Error1: the output file could not be opened!\n");
    exit (1);
for(i = 0; i < INT_SIZE; i++)</pre>
  fscanf(out_file, "%d%d", &i, &rule[2*i+1]);
fclose(out_file);
 \star initialize the noise generator seeds in order to have the same data and
 * noise for different random interleavers
s1 = SEED1;
s2 = SEED2;
 * start the big loop:
for(block = 1; total_err < MAX_ERRORS; block++)</pre>
  {
    jat_code1->enc_state = 0;
                                                   /* reset encoder1's state
    jat_code2->enc_state = 0;
for(i = 0; i < INT_SIZE; i++)</pre>
                                                   /* reset encoder2's state
                                                   /* no app for first decoder */
      D1_app[i] = 1.0;
     * generate random data:
     */
    for(i = 0; i < INT SIZE; i++)
      data[i] = nrgenbin();
    * encoder1:
    */
    for(i = 0; i < INT_SIZE; i++)
      Encl[i] = jat_enc_bp_fp(jat_code1, data[i]);
    * interleave data:
    */
    for(i = 0; i < INT_SIZE; i++)</pre>
     data_i[i] = data[i];
    r_ileava(data_i, rule);
     * encoder2:
    for(i = 0; i < INT_SIZE; i++)
```



```
Enc2[i] = jat_enc_bp_fp(jat_code2, data_i[i]);
    * deinterleave data:
   for(i = 0; i < INT_SIZE; i++)
     data d[i] = data[i];
    r_deileava(data_d, rule);
    * modulate and add AWGN noise:
#ifdef R12_4AM
       /*
        * Channel:
        * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1) = 01--00-(-10--11)
                                                     -3 -1 1 3
   n = (-1.0) / (2 * SIGMA_12_4AM * SIGMA_12 4AM);
   for (i = 0; i < INT SIZE; \overline{i++})
       d0 = data[i];
       if(i & 0x1)
        d1 = Encl[i];
       else
        d1 = Enc2[i];
       tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
       rx = tx + SIGMA_12_4AM * gasdev();
       L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
                 (\exp(n^*(rx+1)^*(rx+1))+\exp(n^*(rx+3)^*(rx+3))));
       L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
                 (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1))));
       D1_data[i] = L_d0;
       if(i & 0x1)
           D1_parity[i] = L d1;
           D2_parity[i] = 0.0;
       else
         {
           D1 parity[i] = 0.0;
           D2_parity[i] = L_d1;
#endif
#ifdef R13 8AM
   /*
    * d0 is MSB and d2 is LSB in 8-AM:(d0,d1,d2):
           *
    */
   n = (-1.0) / (2 * SIGMA_13_8AM * SIGMA_13_8AM);
   for (i = 0; i < INT SIZE; i++)
     {
       d0 = data[i];
       if(i & 0x1)
          d1 = Enc1[i];
           d2 = Enc2[i];
       else
          d1 = Enc2[i];
          d2 = Enc1[i];
```

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}
                       = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
              rx = tx + SIGMA_{13_8AM} * gasdev();

L_{d0} = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.5)*(rx-1.
                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                   (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
              L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                     exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                                   (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
              L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                     \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))/
                                   (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
              D1 data[i] = L d0;
              if(i & 0x1)
                      Dl_parity[i] = L dl;
                      D2_parity[i] = L_d2;
                  }
              else
                  {
                      D1 parity[i] = L d2;
                      D2 parity[i] = L d1;
#endif
#ifdef R12 8AM
       ·/*
         * Channel:
             d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
                        010---011---001---000---100---101---111---110
                       -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
          */
       /*
         \star Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
         * 6 info bits and 6 parity bits are mapped to 2 64QAM symbols which in
          * turn are simulated as 4 8AM symbols to achieve 3bit/s/Hz \,
          * INT_SIZE to be a multiple of 6
             = (-1.0) / (2 * SIGMA_12_8AM * SIGMA_12_8AM);
        for(i = 0; i < INT SIZE; \overline{i}++\overline{i}
           {
               /* symbol 1 */
               d0 = data[i];
               d1 = data[i+1];
              d2 = Encl[i];
                     = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
                       = tx + SIGMA 12 8AM * gasdev();
              L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                   (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                    \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
              L_dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                   (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
              L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                    \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                   (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
```

OMPUTER PROGRAM LISTING APIDIX

```
D1_data[i]
                            = L_d0;
                            = L d1;
 D1 data[i+1]
D1_parity[i]
                            = L_d2;
D1_parity[i+1] = 0;
D2_parity[i]
                            = 0:
 /* symbol 2 */
 d0
        = data[i+2];
 d1
          = Enc1[i+2];
         = Enc2[i+1];
d2
tх
         = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
          = tx + SIGMA 12 8AM * gasdev();
rx
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)));
L_dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                    (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
 D1 data[i+2]
                           = L_d0;
D1_parity[i+2] = L_d1;
D2_parity[i+1] = L_d2;
D2_parity[i+2] = 0;
 /* symbol 3 */
 d0
        = data[i+3];
 d1
          = data[i+4];
d2
         = Enc2[i+3];
         = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
tx
        = tx + SIGMA 12 8AM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                      \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                      \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5))) +
                     \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                    (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
 D1 data[i+3]
                            = L_d0;
 D1 data[i+4]
                            = L d1;
D2 parity[i+3] = L d2;
D1_parity[i+3] = 0;
D2_parity[i+4] = 0;
 /* symbol 4 */
 0.6
          = data[i+5];
 d1
          = Encl[i+4];
d2
         = Enc2[i+5];
         = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_{12_8AM} * gasdev();

L_{d0} = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
```

```
\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
                           L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                                                  \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                                                (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
                           D1_data[i+5] = L_d0;
D1_parity[i+4] = L_d1;
                           D2 parity[i+5] = L d2;
                           D1_parity[i+5] = 0;
                           i = i + 5;
#endif
 #ifdef R23 8AM
                  * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
                                         010--011--001--000--100--101--111--110
-3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
                  */
             n = (-1.0) / (2 * SIGMA 23_8AM * SIGMA 23_8AM);
              for (i = 0; i < INT SIZE; \overline{i++})
                    {
                          d0 = data[i];
                         d1 = data[i+1];
                          if(i & 0x4)
                                d2 = Enc1[i];
                           else
                                d2 = Enc2[i];
                                        = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
                                      = tx + SIGMA_23_8AM * gasdev();
                         rx
                         L d0 = log((exp(n^{+}(rx-0.5)) + (rx-0.5)) + exp(n^{+}(rx-1.5)) + (rx-1.5)) + exp(n^{+}(rx-1.5)) + exp(n^{+}(rx-
                                                                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                                                (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                                                  exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));
                         L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                                                                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                                                (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
                         L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                                                  \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                                                (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
                                                                  = L_d0;
                         D1 data[i]
                         Dl data[i+1] = L d1;
                         if(i & 0x4)
                                        D1 parity[i] = L d2;
                                        D1_parity[i+1] = 0;
                                        D2_parity[i] = 0;
                                       D2 parity[i+1] = 0;
                         else
                                       D1 parity[i] = 0;
                                       D1_parity[i+1] = 0;
                                       D2 parity[i] = L d2;
                                       D2 parity[i+1] = 0;
#endif
```



```
#ifdef R35_32QAM
         * I dimension:
         * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
                      * Q dimension:
         * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1):
                       01----00----11
                     -1.5 -0.5 0.5
         * We transmit one 8AM symbol and one 4AM symbol to emulate a 32QAM symbol.
         \star 6 info bits and 4 parity bits are mapped to 2 32QAM symbols.
         * INT SIZE to be a multiple of 6
       for(i = 0; i < INT SIZE; i++)
               /* symbol 1: 8AM */
            = data[i];
       d1 = data[i+2];
              d2 = Enc1[i];
              tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
       rx = tx + SIGMA_8AM_of_32QAM * gasdev();
              n = (-1.0) / (2 * SIGMA_8AM_of_32QAM * SIGMA_8AM_of_32QAM);
             L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                    \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
             L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
             L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) + exp(n*(rx+1.5)) + 
                                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
              D1 data[i]
                                          = L_d0;
                                          = L_d1;
              D1 data[i+2]
                                          = L d2;
              D1 parity[i]
              D1_parity[i+1] = 0.0;
              D1_parity[i+2] = 0.0;
                                         = 0.0;
              D2_parity[i]
              D2_parity[i+2] = 0.0;
               /* symbol 2: 4AM */
              d0 = data[i+1];
              d1 = Enc2[i+1];
              tx = d0 - d1 + 2*d0*d1 - 0.5;
                     = tx + SIGMA_4AM_of_32QAM * gasdev();
                   = (-1.0) / (2 * SIGMA_4AM_of_32QAM * SIGMA_4AM_of_32QAM);
              L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
              L d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5))*(rx-1.5))) /
                                  (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
              D1 data[i+1]
                                       = L d0;
              D2_parity[i+1] = L_d1;
               /* symbol 3: 8AM */
              = data[i+3];
       d1
               = data[i+5];
              d2 = Enc2[i+4];
                     = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
              tx
             = tx + SIGMA_8AM_of_32QAM * gasdev();
                   = (-1.0) / (2 * SIGMA_8AM_of_32QAM * SIGMA_8AM_of_32QAM);
```



```
L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)));
       L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
       L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
        D1_data[i+3]
                     = L d1;
        D1 data[i+5]
       D1_parity[i+4] = 0.0;
       D1_parity[i+5] = 0.0;
       D2_parity[i+3] = 0.0;
       D2 parity[i+4] = L d2;
       D2_parity[i+5] = 0.0;
        /* symbol 4: 4AM */
       d0 = data[i+4];
       d1 = Enc1[i+3];
       tx = d0 - d1 + 2*d0*d1 - 0.5;
       rx = tx + SIGMA 4AM of 32QAM * gasdev();
          = (-1.0) / (2 * SIGMA_4AM_of_32QAM * SIGMA_4AM_of_32QAM);
       L_{d0} = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
                  (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
       L_dl = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5))*(rx-1.5))) /
                  (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1_data[i+4] = L_d0;
       D1 parity[i+3] = L d1;
       i = i+5;
#endif
#ifdef R46_64QAM_TTCM_VoCAL
    /* Option 4
     * Channel: I & Q defined as
            -|----|----|----|----|----|-
            -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
     * the 64QAM symbol is defined as: (u1, u2, u3, u4, u5, u6)
     * where u4 = d0
            u3 = d1
             u2 = p0 parity from ENC_H
            ul = ql parity from ENC_V
             u5 = d uncoded
            u6 = d uncoded
     * Use s4096v interleaver - only first 2048 bits are interleaved
      = (-1.0) / (2 * SIGMA 46 64QAM * SIGMA 46 64QAM);
    for (i = 0; i < INT SIZE/2 -1;)
       /* Encode only first half of INT_SIZE
        * d0, d1, d2, d3,...
                               up to INT SIZE/2 - 1
        * p0, 0, p2, 0,...
           0, q1, 0, q3,...
        */
       u4 = data[i];
       u3 = data[i+1];
       u2 = Enc1[i];
       u1 = Enc2[i+1];
       u5 = data(i+INT SIZE/21;
       u6 = data[i+INT_SIZE/2+1];
       k = u6+2*u5+4*u4+8*u3+16*u2+32*u1:
```



```
tx_I = find_tx_I(k);
tx_Q = find_tx_Q(k);
rx I = tx I + SIGMA 46 64QAM * gasdev();
rx_Q = tx_Q + SIGMA_46_64QAM * gasdev();
L_d0 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5)))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q-3.5)*(rx Q-3.5))) +
            \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5)))
            \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-2.5)*(rx_Q-2.5)))
                                            (rx_Q-2.5)*(rx_Q-2.5))
            exp(n*((rx I+0.5)*(rx I+0.5))
            \exp(n*((rx_{I-1.5})*(rx_{I-1.5}) + (rx_{Q-2.5})*(rx_{Q-2.5}))) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5))
                                         + (rx_Q-2.5)*(rx_Q-2.5)))
            exp(n*((rx I+3.5)*(rx I+3.5))
                                            (rx Q-1.5)*(rx Q-1.5))
            \exp(n*((rx_{I+1.5})*(rx_{I+1.5}))
                                            (rx_Q-1.5)*(rx_Q-1.5)))
            exp(n*((rx_I-0.5)*(rx_I-0.5))
                                            (rx_Q-1.5)*(rx_Q-1.5))
                                            (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_1-2.5)*(rx_1-2.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx_I+2.5)*(rx_I+2.5))
            \exp(n*((rx^{-1}+0.5)*(rx^{-1}+0.5))
                                            (rx Q-0.5)*(rx Q-0.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5))
            \exp(n*((rx_I-3.5)*(rx_I-3.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx^I+3.5)*(rx^I+3.5))
                                            (rx_Q+0.5)*(rx_Q+0.5))
                                            (rx_Q+0.5)*(rx_Q+0.5))
            exp(n*((rx_I+1.5)*(rx_I+1.5))
            \exp(n*((rx_1-0.5)*(rx_1-0.5))
                                            (rx_Q+0.5)*(rx_Q+0.5))
                                            (rx_Q+0.5)*(rx_Q+0.5))
            exp(n*((rx_1-2.5)*(rx_1-2.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_1+2.5)*(rx_1+2.5))
            exp(n*((rx_I+0.5)*(rx_I+0.5)
                                            (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_I-1.5)*(rx_I-1.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))
                                            (rx_Q+1.5) * (rx_Q+1.5)))
            \exp(n*((rx_1-3.5)*(rx_1-3.5))
                                            (rx_Q+2.5)*(rx_Q+2.5))
            exp(n*((rx_I+3.5)*(rx_I+3.5))
                                         +
                                            (rx_Q+2.5) * (rx_Q+2.5)))
            exp(n*((rx I+1.5)*(rx I+1.5))
            \exp(n*((rx_1-0.5)*(rx_1-0.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx_1-2.5)*(rx_1-2.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
            exp(n*((rx_1+2.5)*(rx_1+2.5))
                                            (rx_Q+3.5)*(rx_Q+3.5))
           \exp(n*((rx_1+0.5)*(rx_1+0.5))
                                            (rx_Q+3.5)*(rx_Q+3.5))
                                         +
            \exp(n*((rx^{T}-1.5)*(rx^{T}-1.5) +
                                            (rx Q+3.5)*(rx Q+3.5))) +
                                            (rx_Q+3.5)*(rx_Q+3.5))))
           \exp(n*((rx_I-3.5)*(rx_I-3.5) +
           (\exp(n*((rx_I+2.5)*(rx_I+2.5))
                                            (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_I+0.5)*(rx_I+0.5)) +
                                            (rx_Q-3.5)*(rx_Q-3.5))) +
            exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q-3.5)*(rx_Q-3.5))
                                            (rx_Q-3.5)*(rx_Q-3.5))
           \exp(n*((rx_I-3.5)*(rx_I-3.5) +
           \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx^Q-2.5)*(rx^Q-2.5))
           exp(n*((rx_I-0.5)*(rx_I-0.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            exp(n*((rx_I-2.5)*(rx_I-2.5))
                                            (rx Q-2.5)*(rx Q-2.5))
                                            (rx_Q-1.5)*(rx_Q-1.5))
           \exp(n*((rx_1+2.5)*(rx_1+2.5)) +
           \exp(n*((rx_1+0.5)*(rx_1+0.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
           exp(n*((rx I-1.5)*(rx I-1.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx I+3.5)*(rx I+3.5) + (rx Q-0.5)*(rx Q-0.5)))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           exp(n*((rx_1-0.5)*(rx_1-0.5))
                                         +
                                            (rx_Q-0.5)*(rx_Q-0.5))
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+0.5)*(rx_Q+0.5)))
           \exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_I-1.5)*(rx_I-1.5)) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx_I+1.5)*(rx_I+1.5))+
                                            (rx Q+1.5)*(rx Q+1.5))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           exp(n*((rx I-2.5)*(rx I-2.5))
                                         + (rx_Q+1.5)*(rx_Q+1.5))
           \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                                            (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx_I+0.5)*(rx_I+0.5))
                                         +
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+2.5)*(rx_Q+2.5)))
            \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+3.5)*(rx_Q+3.5)))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q+3.5)*(rx_Q+3.5)))));
```



```
L d1 = log((exp(n*((rx I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5)))) +
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx I-1.5)*(rx I-1.5)) + (rx Q-3.5)*(rx Q-3.5)))
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q-1.5)*(rx Q-1.5)))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           exp(n*((rx I-2.5)*(rx I-2.5) +
                                            (rx Q-1.5)*(rx Q-1.5))
           \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+0.5)*(rx_Q+0.5)))
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q+0.5)*(rx_Q+0.5)))
                                            (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) +
           \exp(n*((rx^{-1}+0.5)*(rx^{-1}+0.5) + (rx^{-0}+0.5)*(rx^{-0}+0.5)))
           \exp(n*((rx_I^{-1}-0.5)*(rx_I^{-0}-0.5) + (rx_Q^{+0}-0.5)*(rx_Q^{+0}-0.5)))
            exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+0.5)*(rx_Q+0.5)))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+0.5)*(rx_Q+0.5)))
           \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
           exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+2.5)*(rx_Q+2.5)))) /
           (\exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx I+2.5)*(rx I+2.5) + (rx Q-2.5)*(rx Q-2.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx^T+0.5)*(rx^T+0.5) + (rx^T-2.5)*(rx^T-2.5)))
           \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q-2.5)*(rx Q-2.5))) +
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx_Q-2.5)))
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-2.5)*(rx_Q-2.5)))
           \exp(n*((rx I-3.5)*(rx I-3.5) + (rx Q-2.5)*(rx Q-2.5)))
           \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx I+1.5)*(rx I+1.5) + (rx Q-0.5)*(rx Q-0.5)))
           \exp(n*((rx I+0.5)*(rx I+0.5) + (rx Q-0.5)*(rx Q-0.5)))
           \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx I+1.5)*(rx I+1.5) + (rx Q+1.5)*(rx Q+1.5)))
           \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx I+3.5)*(rx I+3.5) + (rx Q+3.5)*(rx Q+3.5)))
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q+3.5)*(rx_Q+3.5)))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5)))
            exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx I-1.5)*(rx I-1.5) + (rx Q+3.5)*(rx Q+3.5))) +
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+3.5)*(rx_Q+3.5)))));
L_d2 = log((exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5)))) +
           \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
```



```
\exp(n*((rx I-2.5)*(rx I-2.5)) + (rx Q-2.5)*(rx Q-2.5))) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
            \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
                                             (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_1+2.5)*(rx_1+2.5))
            \exp(n*((rx_I-0.5)*(rx_I-0.5))
                                             (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx I-1.5)*(rx I-1.5))
                                             (rx Q-1.5)*(rx Q-1.5))
            exp(n*((rx_I+3.5)*(rx_I+3.5)
                                             (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx_I+2.5)*(rx_I+2.5))
                                             (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx^{T}-0.5)*(rx^{T}-0.5))
                                             (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5))
                                          +
                                             (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx_I-3.5)*(rx_I-3.5))
                                          +
                                             (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx_I-2.5)*(rx_I-2.5))
                                             (rx_Q+0.5)*(rx_Q+0.5))
                                          +
            \exp(n*((rx^{I+1.5})*(rx^{I+1.5}) +
                                             (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx_I+0.5)*(rx_I+0.5))
                                             (rx_Q+0.5)*(rx_Q+0.5))
                                          +
                                             (rx_Q+1.5) * (rx_Q+1.5)))
(rx_Q+1.5) * (rx_Q+1.5)))
            exp(n*((rx I+0.5)*(rx I+0.5))
            \exp(n*((rx^{I+1.5})*(rx^{I+1.5}))
            \exp(n*((rx_1-2.5)*(rx_1-2.5))
                                          +
                                             (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_1-3.5)*(rx_1-3.5))
                                          +
                                             (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_I+3.5)*(rx_I+3.5))
                                             (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx^{-1}+2.5)*(rx^{-1}+2.5))
                                             (rx_Q+2.5)*(rx_Q+2.5))) +
            exp(n*((rx_I-1.5)*(rx_I-1.5)
                                             (rx_Q+2.5)*(rx_Q+2.5))) +
                                             (rx_Q+2.5)*(rx_Q+2.5)))
            \exp(n*((rx_I-0.5)*(rx_I-0.5))
            \exp(n*((rx^{-1}-0.5)*(rx^{-1}-0.5))
                                             (rx_Q+3.5) * (rx_Q+3.5)))
                                          +
            exp(n*((rx_I-1.5)*(rx_I-1.5))
                                          +
                                             (rx Q+3.5)*(rx Q+3.5)))
            exp(n*((rx_I+2.5)*(rx_I+2.5)
                                           +
                                             (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_I+3.5)*(rx_I+3.5))
                                             (rx_Q+3.5)*(rx_Q+3.5)))) /
                                          +
           (exp(n*((rx_I+3.5)*(rx_I+3.5))
                                             (rx^Q-3.5)*(rx^Q-3.5))) +
            exp(n*((rx_1+2.5)*(rx_1+2.5))
                                             (rx_Q-3.5)*(rx_Q-3.5))) +
            exp(n*((rx_I-0.5)*(rx_I-0.5))
                                             (rx Q-3.5)*(rx Q-3.5)))
            exp(n*((rx_I-1.5)*(rx_I-1.5)
                                             (rx_Q-3.5)*(rx_Q-3.5))
            exp(n*((rx_I+3.5)*(rx_I+3.5)
                                          +
                                             (rx_Q-2.5)*(rx_Q-2.5)))
                                             (rx_Q-2.5) * (rx_Q-2.5)))
            exp(n*((rx I+2.5)*(rx I+2.5))
                                          +
            exp(n*((rx_I-0.5)*(rx_I-0.5)
                                             (rx_Q-2.5)*(rx_Q-2.5))
                                          +
            exp(n*((rx I-1.5)*(rx I-1.5))
                                             (rx Q-2.5)*(rx Q-2.5))) +
            exp(n*((rx_I+1.5)*(rx_I+1.5)
                                             (rx_Q-1.5)*(rx_Q-1.5))
                                          +
            exp(n*((rx_I+0.5)*(rx_I+0.5))
                                           +
                                             (rx_Q-1.5)*(rx_Q-1.5))
                                             (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx^{I-2.5})*(rx^{I-2.5}) +
            \exp(n*((rx_I^3-3.5)*(rx_I^3-3.5))
                                             (rx_Q-1.5)*(rx_Q-1.5))
                                          +
            exp(n*((rx_I+1.5)*(rx_I+1.5)
                                             (rx_Q-0.5)*(rx_Q-0.5))
                                             (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx I+0.5)*(rx I+0.5)) +
            exp(n*((rx_I-2.5)*(rx_I-2.5))
                                          +
                                             (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx_I-3.5)*(rx_I-3.5))
                                          +
                                             (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx^{T}-1.5)*(rx^{T}-1.5))
                                             (rx Q+0.5)*(rx Q+0.5))
                                          +
            exp(n*((rx I-0.5)*(rx I-0.5) +
                                             (rx_Q+0.5)*(rx_Q+0.5))
            exp(n*((rx_I+2.5)*(rx_I+2.5))
                                          +
                                             (rx_Q+0.5)*(rx_Q+0.5))
                                             (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx I+3.5)*(rx I+3.5))
                                             (rx_Q+1.5) * (rx_Q+1.5)))
            \exp(n*((rx^{I}+3.5)*(rx^{I}+3.5)) +
            exp(n*((rx_I+2.5)*(rx_I+2.5))
                                             (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_1-0.5)*(rx_1-0.5))
                                          +
                                             (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_I-1.5)*(rx_I-1.5)
                                             (rx_Q+1.5)*(rx_Q+1.5))
                                          +
            \exp(n*((rx^{T}+1.5)*(rx^{T}+1.5)) +
                                             (rx Q+2.5)*(rx Q+2.5))
            exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                             (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx_1-2.5)*(rx_1-2.5))
                                             (rx^Q+2.5)*(rx^Q+2.5))
            exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
            exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_1+1.5)*(rx_1+1.5) + (rx_Q+3.5)*(rx_Q+3.5)))));
L_d3 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5)) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-1.5)*(rx_Q-1.5)))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-1.5)*(rx_Q-1.5)))
            \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-1.5)*(rx_Q-1.5)))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
```

```
\exp(n*((rx I-0.5)*(rx_I-0.5) + (rx_Q-0.5)*(rx Q-0.5))) +
                   \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
                   \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
                   \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
                   \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                   \exp(n*((rx^{T}l+2.5)*(rx^{T}l+2.5)) + (rx^{Q}l+2.5)*(rx^{Q}l+2.5))) +
                   \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                   \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                   \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q+2.5)*(rx Q+2.5)))
                   \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                   \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                   \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+2.5)*(rx_Q+2.5)))
                   \exp(n*((rx I+3.5)*(rx_I+3.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
                   \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q+3.5)*(rx_Q+3.5)))
                   \exp(n*((rx I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5)))
                   \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5)))
                   \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+3.5)*(rx_Q+3.5)))
                   \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5)))
                   \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
                   \exp(n*((rx I-3.5)*(rx I-3.5) + (rx Q+3.5)*(rx Q+3.5))))
                  (\exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
                   \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-2.5)*(rx_Q-2.5)))
                   \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-2.5)*(rx_Q-2.5)))
                   \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-2.5)*(rx_Q-2.5)))
                   \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
                   \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx_Q-2.5)))
                   \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
                   exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-2.5)*(rx_Q-2.5)))
                   exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5)))
                   \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-3.5)*(rx_Q-3.5)))
                   \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5)))
                   \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
                   \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-3.5)*(rx_Q-3.5)))
                   \exp(n*((rx I-1.5)*(rx I-1.5) + (rx Q-3.5)*(rx Q-3.5)))
                   \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5)))
                   \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-3.5)*(rx_Q-3.5)))
                   \exp(n*((rx^{T}+3.5)*(rx^{T}+3.5) + (rx^{Q}+1.5)*(rx^{Q}+1.5)))
                   \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+1.5)*(rx_Q+1.5)))
                   \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+1.5)*(rx_Q+1.5)))
                   \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
                   \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
                   \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+1.5)*(rx_Q+1.5)))
                   \exp(n*((rx^TI-2.5)*(rx^TI-2.5) + (rx^TQ+1.5)*(rx^TQ+1.5)))
                   \exp(n*((rx I-3.5)*(rx I-3.5) + (rx Q+1.5)*(rx Q+1.5)))
                   \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+0.5)*(rx_Q+0.5)))
                   \exp(n*((rx I+2.5)*(rx I+2.5) + (rx Q+0.5)*(rx Q+0.5)))
                   \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
                   exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
                   exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
                   \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
                   \exp(n*((rx I-2.5)*(rx I-2.5) + (rx Q+0.5)*(rx Q+0.5))) +
                   \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+0.5)*(rx_Q+0.5))));
       D1 data[i]
                       = L_d3;
                      = L_d2;
       D1_data[i+1]
       D1_data[i + INT SIZE/2]
                                    = rx I;
       D1 data[i + INT SIZE/2 + 1] = rx Q;
                       = L_d1;
       D1 parity[i]
       D1_parity[i+1] = 0;
       D2 parity[i]
                       = 0;
       D2_parity[i+1] = L_d0;
       i = i + 2;
#endif
#ifdef R46_64QAM_TTCM_Ungerboeck Map
    /* Option3: conventional set partitioning used in TCM
     * Channel: I & Q defined
             -|----|----|----|----|----|----|-
```



```
-3.5 -2.5 -1.5 -0.5
                                0.5 1.5
                                              2.5
 * the 64QAM symbol is defined as: (u1, u2, u3, u4, u5, u6)
  where
         u6 = d0
         u5 = d1
         u4 = d2
         u3 = d3
         u2 = p0 parity from ENC_H
         u1 = q1 parity from ENC_V
*/
* deinterleave data:
*/
for(i = 0; i < INT_SIZE; i++)
  data d[i] = data[i];
r_deileava(data_d, rule);
n = (-1.0) / (2 * SIGMA_46_64QAM * SIGMA_46_64QAM);
for(i = 0; i < INT SIZE;)
   /* Puncturing patern is:
    * d0, d1, d2/ d3,...
    * p0, 0, 0, 0,...
       0, 0, q2, 0,...
    */
   u1 = Encl[i];
   u2 = Enc2[i];
   u6 = data_d[i+3];
   u5 = data_d[i+2];
   u4 = data_d[i+1];
   u3 = data_d[i];
   k = u6+2*u5+4*u4+8*u3+16*u2+32*u1;
   tx_I = find_tx_I(k);
   tx_Q = find_tx_Q(k);
   rx_I = tx_I + SIGMA_46_64QAM * gasdev();
   rx_Q = tx_Q + SIGMA_46_64QAM * gasdev();
   L_d0 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5)))) +
               \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
               \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
               \exp(n*((rx^{T}-2.5)*(rx^{T}-2.5) + (rx^{Q}-3.5)*(rx^{Q}-3.5))) +
               \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
               \exp(n*((rx I+0.5)*(rx I+0.5) + (rx Q-2.5)*(rx Q-2.5)))
               \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
               \exp(n*((rx_1-3.5)*(rx_1-3.5)) + (rx_Q-2.5)*(rx_Q-2.5)))
               \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q-1.5)*(rx_Q-1.5)))
               \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-1.5)*(rx_Q-1.5)))
               \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q-1.5)*(rx Q-1.5)))
               \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-1.5)*(rx_Q-1.5)))
               \exp(n*((rx I+2.5)*(rx I+2.5) + (rx Q-0.5)*(rx Q-0.5)))
               \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-0.5)*(rx_Q-0.5)))
               \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-0.5)*(rx_Q-0.5)))
               \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
               \exp(n*((rx I+3.5)*(rx I+3.5) + (rx Q+0.5)*(rx Q+0.5)))
               \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+0.5)*(rx_Q+0.5)))
               \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+0.5)*(rx_Q+0.5)))
               \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q+0.5)*(rx_Q+0.5)))
               \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+1.5)*(rx_Q+1.5)))
               exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
               \exp(n*((rx_1-1.5)*(rx_1-1.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
               \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
               \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
               \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
               \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
               \exp(n*((rx_I-2.5)*(rx_I-2.5)) + (rx_Q+2.5)*(rx_Q+2.5))) +
               \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
               \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
               \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
```



```
\exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+3.5)*(rx_Q+3.5)))))
           (\exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
                                           (rx_Q-3.5)*(rx_Q-3.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) +
            exp(n*((rx_I-3.5)*(rx_I-3.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))
            \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                           (rx Q-2.5)*(rx Q-2.5))
                                           (rx_Q-2.5)*(rx_Q-2.5))
            exp(n*((rx_I+1.5)*(rx_I+1.5) +
            \exp(n*((rx_I^-0.5)*(rx_I^-0.5))
                                        +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-2.5)*(rx_Q-2.5)))
            \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-1.5)*(rx_Q-1.5)))
            exp(n*((rx_1+0.5)*(rx_1+0.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
            exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                           (rx^Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
            \exp(n*((rx_I+1.5)*(rx_I+1.5)) +
                                            (rx Q-0.5)*(rx Q-0.5))
           \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
            \exp(n*((rx_1+2.5)*(rx_1+2.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
            exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                           (rx Q+0.5)*(rx Q+0.5))
                                           (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_I-3.5)*(rx_I-3.5) +
           \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                           (rx_Q+1.5)*(rx_Q+1.5))
           \exp(n*((rx I+1.5)*(rx I+1.5) +
                                           (rx_Q+1.5)*(rx_Q+1.5))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            exp(n*((rx_I-2.5)*(rx_I-2.5) +
                                           (rx_Q+1.5)*(rx_Q+1.5))
           exp(n*((rx_1+2.5)*(rx_1+2.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
           exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx I-3.5)*(rx I-3.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+3.5)*(rx_Q+3.5)))));
L_dl = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5)))) +
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx I+1.5)*(rx I+1.5) + (rx Q-3.5)*(rx Q-3.5))) +
           \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx_1-0.5)*(rx_1-0.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5)))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
           \exp(n*((rx_1+2.5)*(rx_1+2.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
           exp(n*((rx_1+0.5)*(rx_1+0.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
           \exp(n*((rx_I^-1-0.5)*(rx_I^-0.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))) +
                                           (rx_Q-1.5)*(rx_Q-1.5))) +
           exp(n*((rx I-1.5)*(rx I-1.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
           exp(n*((rx_I-2.5)*(rx_I-2.5) +
           \exp(n*((rx I-3.5)*(rx I-3.5) +
                                           (rx_Q-1.5)*(rx_Q-1.5))
           exp(n*((rx I+3.5)*(rx I+3.5) +
                                           (rx Q+0.5)*(rx Q+0.5))
           \exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx I+1.5)*(rx I+1.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
                                           (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_1+0.5)*(rx_1+0.5)) +
           exp(n*((rx_I-0.5)*(rx_I-0.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx I-1.5)*(rx I-1.5) +
           \exp(n*((rx I-2.5)*(rx I-2.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                           (rx_Q+0.5)*(rx_Q+0.5))
           exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5)))
           exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                           (rx Q+2.5)*(rx Q+2.5))
                                           (rx_Q+2.5)*(rx_Q+2.5))) +
           \exp(n*((rx^{I+1.5})*(rx^{I+1.5}) +
           \exp(n*((rx I+0.5)*(rx I+0.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))) +
                                           (rx_Q+2.5)*(rx_Q+2.5))) +
           exp(n*((rx_I-0.5)*(rx_I-0.5) +
           \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
                                           (rx_Q+2.5)*(rx_Q+2.5))) +
           \exp(n*((rx^{-1}-2.5)*(rx^{-1}-2.5) +
           \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5)))) /
           (\exp(n*((rx^I+3.5)*(rx^I+3.5)) +
                                           (rx_Q-2.5)*(rx_Q-2.5))) +
                                           (rx_Q-2.5)*(rx_Q-2.5))) +
           exp(n*((rx_I+2.5)*(rx_I+2.5) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                           (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx I-0.5)*(rx_I-0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
```

COMPUTER PROGRAM LISTING APENDIX

```
exp(n*((rx I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx Q-2.5))) +
            \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
            exp(n*((rx_I+3.5)*(rx_I+3.5)
                                            (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_1+2.5)*(rx_1+2.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx^{T}+1.5)*(rx^{T}+1.5) +
                                            (rx^Q-0.5)*(rx^Q-0.5))) +
            exp(n*((rx_I+0.5)*(rx_I+0.5)
                                            (rx^Q-0.5)*(rx^Q-0.5))
                                         +
            exp(n*((rx_I-0.5)*(rx_I-0.5))
                                            (rx^{Q-0.5})*(rx^{Q-0.5}))
            \exp(n*((rx^{T}-1.5)*(rx^{T}-1.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx_1-2.5)*(rx_1-2.5) +
                                            (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx_I-3.5)*(rx_I-3.5)
                                         +
                                            (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx^I+3.5)*(rx_I+3.5))
                                         +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_1+2.5)*(rx_1+2.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))
                                         +
            exp(n*((rx I+0.5)*(rx I+0.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))
                                          +
           \exp(n*((rx_{I-0.5})*(rx_{I-0.5}) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                           (rx_Q+1.5)*(rx_Q+1.5))
                                           (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_I-2.5)*(rx_I-2.5) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5))
                                         +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx^{T}+3.5)*(rx^{T}+3.5) +
                                            (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
                                            (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5))
           \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5)))
            \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q+3.5)*(rx Q+3.5))) +
            exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+3.5)*(rx_Q+3.5))));
L_d2 = log((exp(n*((rx I+1.5)*(rx I+1.5) + (rx Q-3.5)*(rx Q-3.5)))) +
           \exp(n*((rx I+0.5)*(rx I+0.5) + (rx Q-3.5)*(rx Q-3.5))) +
           \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx I+0.5)*(rx I+0.5) + (rx Q-2.5)*(rx Q-2.5))) +
           exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_0-2.5)*(rx_0-2.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
           \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-1.5)*(rx_Q-1.5)))
            exp(n*((rx_I-0.5)*(rx_I-0.5) +
                                            (rx^{Q-1.5})*(rx^{Q-1.5}))
           exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx^Q-0.5)*(rx^Q-0.5))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
           \exp(n*((rx I-2.5)*(rx I-2.5) +
                                            (rx Q+0.5)*(rx Q+0.5))
           \exp(n*((rx_1+1.5)*(rx_1+1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
           exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+0.5)*(rx_Q+0.5)))
           exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                           (rx_Q+1.5)*(rx_Q+1.5))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx I-2.5)*(rx I-2.5) + (rx Q+1.5)*(rx Q+1.5)))
           \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx^{T}+2.5)*(rx^{T}+2.5) + (rx^{Q}+2.5)*(rx^{Q}+2.5)))
           exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
           \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q+3.5)*(rx_Q+3.5)))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
           exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
                                           (rx_Q+3.5)*(rx_Q+3.5)))) /
           \exp(n*((rx I+3.5)*(rx I+3.5) +
           (\exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_0-3.5)*(rx_0-3.5))) +
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-3.5)*(rx_Q-3.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-2.5)*(rx_Q-2.5)))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-2.5)*(rx_Q-2.5)))
           exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
           exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
           \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
           \exp(n*((rx_1-2.5)*(rx I-2.5) + (rx Q-1.5)*(rx Q-1.5))) +
```

COMPUTER PROGRAM LISTING PENDIX

```
\exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx_I-3.5)*(rx_I-3.5) +
                                            (rx_Q-0.5)*(rx_Q-0.5))) +
                                            (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx^{-1}-1.5)*(rx^{-1}-1.5) +
            \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx_1+2.5)*(rx_1+2.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_1+2.5)*(rx_1+2.5) +
            \exp(n*((rx^{1}-0.5)*(rx^{1}-0.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5)) +
                                            (rx_Q+1.5)*(rx_Q+1.5))) +
            exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx^{I}+0.5)*(rx^{I}+0.5)) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
           exp(n*((rx I-2.5)*(rx_I-2.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                            (rx_Q+3.5)*(rx_Q+3.5))) +
            exp(n*((rx_1-2.5)*(rx_1-2.5))
                                         +
                                            (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx^{I}+0.5)*(rx^{I}+0.5) +
                                            (rx^Q+3.5)*(rx^Q+3.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5))));
L_d3 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx I+2.5)*(rx I+2.5) + (rx Q-1.5)*(rx Q-1.5))) +
           \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))) +
           exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_I^{-1.5})*(rx_I^{-1.5}) + (rx_Q^{-1.5})*(rx_Q^{-1.5})))
           exp(n*((rx I-2.5)*(rx I-2.5) +
                                            (rx Q-1.5)*(rx Q-1.5))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-1.5)*(rx_Q-1.5)))
           \exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx I+2.5)*(rx I+2.5) +
                                           (rx_Q-0.5)*(rx_Q-0.5))
           \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                           (rx_Q-0.5)*(rx_Q-0.5))
            exp(n*((rx I+0.5)*(rx I+0.5) +
                                           (rx Q-0.5)*(rx Q-0.5))
           \exp(n*((rx_I^-1-0.5)*(rx_I^-1-0.5) +
                                           (rx_Q-0.5)*(rx_Q-0.5))
           \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q-0.5)*(rx_Q-0.5))
           \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
            \exp(n*((rx_1+3.5)*(rx_1+3.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
                                           (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx^{I+2.5})*(rx^{I+2.5}) +
           exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
                                            (rx_Q+2.5)*(rx_Q+2.5))
           exp'(n*((rx I-0.5)*(rx I-0.5) +
           \exp(n*((rx I-1.5)*(rx I-1.5) +
                                           (rx_Q+2.5)*(rx_Q+2.5))
           exp(n*((rx_I-2.5)*(rx_I-2.5) +
                                            (rx_Q+2.5)*(rx_Q+2.5))
           \exp(n*((rx I-3.5)*(rx I-3.5) +
                                            (rx Q+2.5)*(rx Q+2.5))
           \exp(n*((rx^{I+3.5})*(rx^{I+3.5}) +
                                           (rx_Q+3.5)*(rx_Q+3.5))
           \exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                           (rx_Q+3.5)*(rx_Q+3.5))
                                            (rx_Q+3.5)*(rx_Q+3.5))) +
           exp(n*((rx_I+1.5)*(rx_I+1.5) +
           \exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                            (rx_Q+3.5)*(rx_Q+3.5))
           \exp(n*((rx I-0.5)*(rx I-0.5) +
                                            (rx Q+3.5)*(rx Q+3.5))) +
           \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q+3.5)*(rx_Q+3.5))) +
           \exp(n*((rx_I-2.5)*(rx_I-2.5))
                                            (rx^Q+3.5)*(rx^Q+3.5))) +
                                         +
                                            (rx_Q+3.5) * (rx_Q+3.5)))) /
           \exp(n*((rx^{-1}-3.5)*(rx^{-1}-3.5)) +
                                            (rx_Q-2.5)*(rx_Q-2.5))) +
          (\exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))) +
           exp(n*((rx_I+2.5)*(rx_I+2.5)
                                         +
           exp(n*((rx_I+1.5)*(rx_I+1.5))
                                            (rx Q-2.5)*(rx Q-2.5))) +
                                         +
           \exp(n*((rx_1+0.5)*(rx_1+0.5)) +
                                           (rx^Q-2.5)*(rx^Q-2.5))) +
           \exp(n*((rx_1-0.5)*(rx_1-0.5) +
                                           (rx_Q-2.5)*(rx_Q-2.5))) +
           exp(n*((rx I-1.5)*(rx I-1.5) +
                                           (rx Q-2.5)*(rx Q-2.5))) +
           \exp(n*((rx_I-2.5)*(rx_I-2.5) +
                                           (rx_Q-2.5)*(rx_Q-2.5))) +
           exp(n*((rx_I-3.5)*(rx_I-3.5) +
                                           (rx_Q-2.5)*(rx_Q-2.5))) +
           \exp(n*((rx_1+3.5)*(rx_1+3.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))) +
                                           (rx_Q-3.5)*(rx_Q-3.5))
           exp(n*((rx_I+2.5)*(rx_I+2.5)) +
           \exp(n*((rx^{-1}+1.5)*(rx^{-1}+1.5) +
                                           (rx^Q-3.5)*(rx^Q-3.5))) +
           exp(n*((rx_1+0.5)*(rx_1+0.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))) +
           exp(n*((rx_I-0.5)*(rx_I-0.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))) +
           exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                           (rx_Q-3.5)*(rx_Q-3.5))
           exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
           exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
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COMPUTER PROGRAM LISTING APPLINDIX

```
\exp(n*((rx I+2.5)*(rx_I+2.5) + (rx Q+1.5)*(rx Q+1.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx_1-0.5)*(rx_1-0.5)) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_1-1.5)*(rx_1-1.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx I-2.5)*(rx I-2.5) +
                                            (rx Q+1.5)*(rx Q+1.5))
            \exp(n*((rx_1-3.5)*(rx_1-3.5))
                                          + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx^{T}+3.5)*(rx^{T}+3.5))
                                          +
                                            (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx_{I+2.5})*(rx_{I+2.5}) +
                                            (rx Q+0.5)*(rx Q+0.5))
            exp(n*((rx_I+1.5)*(rx_I+1.5)) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
            exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx^{-1}-0.5)*(rx^{-1}-0.5) +
                                            (rx^Q+0.5)*(rx^Q+0.5))
            \exp(n*((rx I-1.5)*(rx I-1.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx I-3.5)*(rx I-3.5) + (rx Q+0.5)*(rx Q+0.5))));
L_d4 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+3.5)*(rx_Q+3.5)))) +
            exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5)))
            \exp(n*((rx^{I}+0.5)*(rx^{I}+0.5) +
                                            (rx Q+3.5)*(rx Q+3.5))) +
            \exp(n*((rx_1-0.5)*(rx_1-0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx_I^-1-1.5)*(rx_I^-1.5))
                                          +
                                            (rx_Q+3.5)*(rx_Q+3.5))
            \exp(n*((rx I-2.5)*(rx I-2.5) + (rx Q+3.5)*(rx Q+3.5)))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+3.5)*(rx_Q+3.5)))
            exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx^Q+1.5)*(rx^Q+1.5))
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            exp(n*((rx I-0.5)*(rx I-0.5))
                                          +
                                            (rx Q+1.5)*(rx Q+1.5))
            \exp(n*((rx I-1.5)*(rx I-1.5) + (rx Q+1.5)*(rx Q+1.5)))
            exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx^{-1}-3.5)*(rx^{-1}-3.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_I+3.5)*(rx_I+3.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
            exp(n*((rx I+2.5)*(rx I+2.5) +
                                            (rx Q+0.5)*(rx Q+0.5))
            exp(n*((rx_I+1.5)*(rx_I+1.5)
                                          + (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx^{I+0.5})*(rx^{I+0.5}))
                                            (rx_Q+0.5)*(rx_Q+0.5))
                                          +
            \exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q+0.5)*(rx Q+0.5)))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+0.5)*(rx_Q+0.5)))
            \exp(n*((rx^{T}1-2.5)*(rx^{T}1-2.5))
                                            (rx^Q+0.5)*(rx^Q+0.5))
                                          +
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q+0.5)*(rx_Q+0.5)))
            exp(n*((rx_I+3.5)*(rx_I+3.5)
                                          + (rx_Q+2.5)*(rx_Q+2.5))) +
                                          + (rx_Q+2.5)*(rx_Q+2.5)))
            exp(n*((rx_I+2.5)*(rx_I+2.5))
            \exp(n*((rx_I+1.5)*(rx_I+1.5))
                                            (rx^Q+2.5)*(rx^Q+2.5))
                                          +
            \exp(n*((rx^{T}+0.5)*(rx^{T}+0.5) + (rx^{Q}+2.5)*(rx^{Q}+2.5)))
            \exp(n*((rx_1-0.5)*(rx_1-0.5))
                                          + (rx_Q+2.5)*(rx_Q+2.5)))
            exp(n*((rx I-1.5)*(rx I-1.5))
                                            (rx Q+2.5)*(rx Q+2.5))) +
                                         + (rx_Q+2.5)*(rx_Q+2.5))) +
            \exp(n*((rx I-2.5)*(rx I-2.5))
            exp(n*((rx_I-3.5)*(rx_I-3.5))
                                          + (rx_Q+2.5)*(rx_Q+2.5)))) /
           (exp(n*((rx_I+3.5)*(rx_I+3.5)
                                            (rx_Q-2.5)*(rx_Q-2.5))) +
            \exp(n*((rx_I+2.5)*(rx_I+2.5))
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx^{T}+1.5)*(rx^{T}+1.5) +
                                            (rx Q-2.5)*(rx Q-2.5))) +
            exp(n*((rx_I+0.5)*(rx_I+0.5))
                                          + (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx_I-0.5)*(rx_I-0.5))
                                            (rx^Q-2.5)*(rx^Q-2.5))
                                            (rx_Q-2.5)*(rx_Q-2.5))) +
            \exp(n*((rx^{I}-1.5)*(rx^{I}-1.5))
                                         +
            \exp(n*((rx_1-2.5)*(rx_1-2.5))
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx_1-3.5)*(rx_1-3.5))
                                          +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx^{I}+3.5)*(rx^{I}+3.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
                                          +
            \exp(n*((rx^{I+2.5})*(rx^{I+2.5}) +
                                            (rx^Q-0.5)*(rx^Q-0.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5))
                                         + (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx^{-1}+0.5)*(rx^{-1}+0.5))
                                            (rx^Q-0.5)*(rx^Q-0.5))
            \exp(n*((rx_1-0.5)*(rx_1-0.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
                                          +
            exp(n*((rx_I-1.5)*(rx_I-1.5))
                                            (rx Q-0.5)*(rx Q-0.5))
                                            (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx_1-2.5)*(rx_1-2.5))
            exp(n*((rx_1-3.5)*(rx_1-3.5))
                                          +
                                            (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx^{I}+3.5)*(rx^{I}+3.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
            exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_1+0.5)*(rx_1+0.5) +
                                            (rx^Q-1.5)*(rx^Q-1.5))
           \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
           \exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
            \exp(n^*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-1.5)*(rx_Q-1.5)))
```



```
exp(n*((rx I-3.5)*(rx I-3.5) + (rx Q-1.5)*(rx_Q-1.5))) +
            \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            exp(n*((rx_1+2.5)*(rx_1+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            \exp(n*((rx_1+1.5)*(rx_1+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            exp(n*((rx I-0.5)*(rx I-0.5) + (rx Q-3.5)*(rx Q-3.5))) +
            exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5) + (rx_Q-3.5)*(rx_Q-3.5)))));
L_d5 = log((exp(n*((rx_1+3.5)*(rx_1+3.5)) + (rx_0+3.5)*(rx_0+3.5))) +
            \exp(n*((rx I+2.5)*(rx I+2.5) + (rx Q+3.5)*(rx Q+3.5))) +
            \exp(n*((rx^{T}+1.5)*(rx^{T}+1.5) + (rx^{Q}+3.5)*(rx^{Q}+3.5))) +
            exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
            \exp(n*((rx I+3.5)*(rx I+3.5) + (rx Q+2.5)*(rx Q+2.5)))
            exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
            exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5)))
            \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q+2.5)*(rx_Q+2.5)))
            exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            \exp(n*((rx I+2.5)*(rx I+2.5) + (rx Q+1.5)*(rx Q+1.5))) +
            \exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+1.5)*(rx_Q+1.5)))
            exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
            \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+0.5)*(rx_Q+0.5)))
            exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))
            \exp(n*((rx_1+0.5)*(rx_1+0.5) + (rx_Q+0.5)*(rx_Q+0.5)))
            \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q-0.5)*(rx_Q-0.5)))
            \exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-0.5)*(rx_Q-0.5)))
            exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx Q-0.5)*(rx Q-0.5))
            \exp(n*((rx I+0.5)*(rx I+0.5) + (rx Q-0.5)*(rx Q-0.5)))
            exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5)))
            exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                            (rx Q-1.5)*(rx Q-1.5))
            exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q-1.5) * (rx_Q-1.5)))
            \exp(n*((rx I+0.5)*(rx I+0.5) + (rx Q-1.5)*(rx Q-1.5)))
            \exp(n*((rx_1+3.5)*(rx_1+3.5) + (rx_Q-2.5)*(rx_Q-2.5)))
            \exp(n*((rx_I+2.5)*(rx_I+2.5) +
                                            (rx^Q-2.5)*(rx^Q-2.5))
            exp(n*((rx^{T}+1.5)*(rx^{T}+1.5) + (rx^{Q}-2.5)*(rx^{Q}-2.5)))
            \exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-2.5)*(rx_Q-2.5)))
            \exp(n*((rx_1+3.5)*(rx_1+3.5) +
                                            (rx_Q-3.5)*(rx_Q-3.5))
            \exp(n*((rx I+2.5)*(rx I+2.5) +
                                            (rx^Q-3.5)*(rx^Q-3.5))
            exp(n*((rx_I+1.5)*(rx_I+1.5) +
                                            (rx_Q-3.5)*(rx_Q-3.5))
            \exp(n*((rx_I+0.5)*(rx_I+0.5) +
                                            (rx_Q-3.5)*(rx_Q-3.5)))) /
           (\exp(n*((rx_1-3.5)*(rx_1-3.5)) +
                                            (rx Q-3.5)*(rx Q-3.5))) +
            \exp(n*((rx_1-2.5)*(rx_1-2.5)) +
                                            (rx_Q^-3.5)*(rx_Q^-3.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q-3.5)*(rx_Q-3.5))
            exp(n*((rx I-0.5)*(rx I-0.5) +
                                            (rx Q-3.5)*(rx Q-3.5))
            exp(n*((rx_1-0.5)*(rx_1-0.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx_I-2.5)*(rx_I-2.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                            (rx_Q-2.5)*(rx_Q-2.5))
            \exp(n*((rx^{-1}-3.5)*(rx^{-1}-3.5) +
                                            (rx Q-1.5)*(rx Q-1.5))
            exp(n*((rx_I-2.5)*(rx_I-2.5) +
                                            (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5))
                                            (rx_Q-1.5)*(rx_Q-1.5))
                                            (rx_Q-1.5)*(rx_Q-1.5))
            \exp(n*((rx^{I}-0.5)*(rx^{I}-0.5) +
            \exp(n*((rx_1-0.5)*(rx_1-0.5) +
                                            (rx_Q-0.5)*(rx_Q-0.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q-0.5)*(rx_Q-0.5))) +
            \exp(n*((rx^{T}-2.5)*(rx^{T}-2.5))
                                            (rx Q-0.5)*(rx Q-0.5))) +
                                         +
            \exp(n*((rx^{1}-3.5)*(rx^{1}-3.5) +
                                            (rx^Q-0.5)*(rx^Q-0.5))) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx I-2.5)*(rx I-2.5))
                                            (rx Q+0.5)*(rx Q+0.5))
            \exp(n*((rx_I-1.5)*(rx_I-1.5) +
                                            (rx_Q+0.5)*(rx_Q+0.5))) +
            \exp(n*((rx_I-0.5)*(rx_I-0.5) +
                                            (rx Q+0.5)*(rx Q+0.5))) +
           exp(n*((rx_I-0.5)*(rx_I-0.5)
exp(n*((rx_I-1.5)*(rx_I-1.5)
                                            (rx_Q+1.5)*(rx_Q+1.5))) +
                                            (rx_Q+1.5)*(rx_Q+1.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))) +
            exp(n*((rx_I-2.5)*(rx_I-2.5) +
            \exp(n*((rx_1-3.5)*(rx_1-3.5))
                                            (rx_Q+1.5)*(rx_Q+1.5))) +
            exp(n*((rx_I-3.5)*(rx_I-3.5))
                                            (rx_Q+2.5)*(rx_Q+2.5))) +
            \exp(n*((rx_I-2.5)*(rx_I-2.5))
                                         +
                                            (rx Q+2.5)*(rx Q+2.5))) +
                                            (rx_Q+2.5)*(rx_Q+2.5))) +
            \exp(n*((rx_I^{-1}-1.5)*(rx_I^{-1}-1.5) +
            \exp(n*((rx_I^{-0.5})*(rx_I^{-0.5}) + (rx_Q^{+2.5})*(rx_Q^{+2.5}))) +
            \exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
```

COMPUTER PROGRAM LISTING ALENDIX

```
\exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
                    \exp(n*((rx_1-2.5)*(rx_1-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
                    \exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+3.5)*(rx_Q+3.5)))));
       D1 data[i]
                       = L_d2;
       D1_data[i+1]
                       = L_d3;
                       = L_d4;
       D1 data[i+2]
       D1_data[i+3]
                       = L_d5;
                      = L_d0;
       D1_parity[i]
       D1_parity[i+1] = 0.0;
       D1_parity[i+2] = 0.0;
       D1_parity[i+3] = 0.0;
       D2_parity[i] = L_d1;
       D2 parity[i+1] = 0.0;
       D2[parity[i+2] = 0.0;
       D2 parity[i+3] = 0.0;
       i = i + 4;
      }
     * interleave data:
    r_ileav(D1_data, rule);
#endif
#ifdef R46_64QAM_IQ_Natural_Map
    /* Option2
    * Channel: I = (u1, u2, u3), Q = (u4, u5, u6) defined using natural mapping: * 000 001 010 011 100 101 110 .111
             -|----|----|----|----|----|----|-
            -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
     * the 64QAM symbol is defined as: (u1, u2, u3, u4, u5, u6)
             u1 = d0
             u2 = d1
             u3 = p0 parity from ENC_V
             u4 = d2
             u5 = d3
             u6 = q0 parity from ENC_H
     */
     * deinterleave data:
    for(i = 0; i < INT_SIZE; i++)</pre>
      data_d[i] = data[i];
    r_deileava(data_d, rule);
   n = (-1.0) / (2 * SIGMA 46 64QAM * SIGMA 46 64QAM);
    for(i = 0; i < INT SIZE;)</pre>
      {
       /* Puncturing patern is:
        * d0, d1, d2, d3,...
* p0, 0, 0, 0,...
        * q0, 0, 0, 0,...
       u1 = data_d[i];
       u2 = data d[i+1];
       u3 = Encl[i];
       u4 = data_d[i+2];
       u5 = data_d[i+3];
       u6 = Enc2[i];
       tx_I = -3.5 + u3 + 2*u2 + 4*u1;
       tx_Q = -3.5 + u6 + 2*u5 + 4*u4;
       rx_I = tx_I + SIGMA_46_64QAM * gasdev();
```



```
rx_Q = tx_Q + SIGMA_46_64QAM * gasdev();
  L_ul = log((exp(n*((rx_I-3.5)*(rx_I-3.5))))+
               \exp(n*((rx_1-2.5)*(rx_1-2.5)))+
               \exp(n*((rx_I-1.5)*(rx_I-1.5)))+
               \exp(n*((rx_1-0.5)*(rx_1-0.5))))
              (\exp(n*((rx_1+3.5)*(rx_1+3.5)))+
               \exp(n*((rx_I+2.5)*(rx_I+2.5)))+
               \exp(n*((rx^{I+1.5})*(rx^{I+1.5})))+
               exp(n*((rx_I+0.5)*(rx_I+0.5)))));
  L_u2 = log((exp(n*((rx_I-3.5)*(rx_I-3.5))))+
               \exp(n*((rx_I-2.5)*(rx_I-2.5)))+
               \exp(n*((rx_I+1.5)*(rx_I+1.5)))+
               \exp(n*((rx_I+0.5)*(rx_I+0.5))))
              (\exp(n*((rx_1+3.5)*(rx_1+3.5)))+
               \exp(n*((rx_I+2.5)*(rx_I+2.5)))+
               exp(n*((rx_I-1.5)*(rx_I-1.5)))+
               \exp(n*((rx_1-0.5)*(rx_1-0.5))));
  L_u3 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
               \exp(n*((rx_I+2.5)*(rx_I+2.5)))+
               exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5)))/
              (\exp(n*((rx_1+3.5)*(rx_1+3.5)))+
               \exp(n*((rx_1-2.5)*(rx_1-2.5)))+
               \exp(n*((rx^I+1.5)*(rx^I+1.5)))+
               exp(n*((rx_I-0.5)*(rx_I-0.5))));
  rx I = rx Q;
  L_u4 = log((exp(n*((rx_I-3.5)*(rx_I-3.5))))+
               exp(n*((rx_I-2.5)*(rx_I-2.5)))+
               \exp(n*((rx_I-1.5)*(rx_I-1.5)))+
               \exp(n*((rx_1-0.5)*(rx_1-0.5))))
              (exp(n*((rx_1+3.5)*(rx_1+3.5)))+
               exp(n*((rx_I+2.5)*(rx_I+2.5)))+
               exp(n*((rx_I+1.5)*(rx_I+1.5)))+
               \exp(n*((rx^I+0.5)*(rx^I+0.5))));
  L_u5 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
               \exp(n*((rx_I-2.5)*(rx_I-2.5)))+
               exp(n*((rx_I+1.5)*(rx_I+1.5)))+
               exp(n*((rx_I+0.5)*(rx_I+0.5))))/
              (exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
               \exp(n*((rx_I-1.5)*(rx_I-1.5)))+
               exp(n*((rx_I-0.5)*(rx_I-0.5)))));
  L_u6 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
               exp(n*((rx_I+2.5)*(rx_I+2.5)))+
               exp(n*((rx_I-1.5)*(rx_I-1.5)))+
              exp(n*((rx_I+0.5)*(rx_I+0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
               \exp(n*((rx I-2.5)*(rx I-2.5)))+
               \exp(n*((rx_I+1.5)*(rx_I+1.5)))+
               exp(n*((rx_I-0.5)*(rx_I-0.5)))));
  D1_data[i]
                  = L_u1;
  D1_data[i+1]
                  = L u2;
  D1 data[i+2]
                  = L_u4;
  D1_data[i+3]
                  = L_u5;
  D1_parity[i]
                  = L_u3;
  D1_parity[i+1] = 0.0;
  D1_parity[i+2] = 0.0;
  D1_parity[i+3] = 0.0;
  D2 parity[i]
                  = L u6;
  D2_parity[i+1] = 0.0;
  D2 parity[i+2] = 0.0;
  D2_parity[i+3] = 0.0;
  i = i + 4;
* interleave data:
```



```
r ileav(D1 data, rule);
#endif
#ifdef R46_64QAM_IQ_Gray_Map
    /* Option1: used in "Parallel Concatenated Trellis Coded Modulation" ICC'96
    * Channel: I = (u1, u2, u3), Q = (u4, u5, u6) defined using Gray mapping:
    * u1 & u4 are MSBs and u3 & u6 are LSBs:
            * where:
             u1 = d0
             u2 = d1
            u3 = p0 parity from ENC_V
            u4 = d2
            u5 = d3
            u6 = q0 parity from ENC_H
      INT_SIZE = multiple of 4
       = (-1.0) / (2 * SIGMA_23_8AM * SIGMA_23_8AM);
    * deinterleave data:
    */
   for (i = 0; i < INT SIZE; i++)
     data d[i] = data[i];
   r_deileava(data_d, rule);
   for(i = 0; i < INT SIZE;)
       /* Puncturing patern is:
        * d0, d1, d2, d3,...
        * p0, 0, 0, 0, ...
* q0, 0, 0, 0,...
                      0,...
        */
       u1
            = data d[i];
            = data d[i+1];
       u2
       u3
            = Enc1[i];
       tх
            = 2*u1 - 2*u2 + 4*u1*u2 - 1.0 + (((2*u1-1)*(2*u2-1))<0?(u3-0.5):(0.5-u3));
           = tx + SIGMA_23_8AM * gasdev();
       rx
       Lu1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)));
       Lu2 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
       L_u3 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
            = data d[i+2];
       u1
            = data_d[i+3];
       u2
       u3
            = Enc2[i];
           = 2*u1 - 2*u2 + 4*u1*u2 - 1.0 + (((2*u1-1)*(2*u2-1))<0?(u3-0.5):(0.5-u3));
       tx
           = tx + SIGMA 23 8AM * gasdev();
       L_u4 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
       L_u5 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
```

```
\exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                   (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
       L u6 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) + rx+1.5))
                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))/
                   (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
       D1_data[i]
D1_data[i+1]
                       = L_u1;
                       = L_u2;
       D1_data[i+2]
                       = L_u4;
       D1_data[i+3]
                      = L_u5;
       D1_parity[i]
                      = L_u3;
       D1_parity[i+1] = 0.0;
       D1_parity[i+2] = 0.0;
       D1_parity[i+3] = 0.0;
       D2_parity[i] = L_u6;
       D2 parity[i+1] = 0.0;
       D2_parity[i+2] = 0.0;
       D2_parity[i+3] = 0.0;
       i = i + 4;
       interleave data:
    r_ileav(D1_data, rule);
#endif
/*mio*/
#ifdef R24_4QAM
    /*
    \star Channel: we transmit two 2-AM symbols to emulate a 4-QAM symbol.
     * 2 info bits and 2 parity bits are mapped to 2 4-QAM symbols which in
   \,\,^{\star} turn are simulated as 4 2-AM symbols to achieve 1bit/s/Hz
     * INT_SIZE to be a multiple of 2
     */
    n = (-1.0) / (2 * SIGMA_24_4QAM * SIGMA_24_4QAM);
    for (i = 0; i < INT SIZE; i++)
      {
        /* symbol 1 */
       d0 = data[i];
        tx
            = d0 - 0.5;
            = tx + SIGMA_24_4QAM * gasdev();
        rx
        L d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                  (exp(n*(rx+0.5)*(rx+0.5))));
        D1_data[i]
                     = L_d0;
        /* symbol 2 */
        d0 = Enc1[i];
           = d0 - 0.5;
        tx
            = tx + SIGMA_24_4QAM * gasdev();
        L d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))));
        D1_parity[i] = L_d0;
        /* symbol 3 */
            = data[i+1];
       d0
            = d0 - 0.5;
             = tx + SIGMA_24_4QAM * gasdev();
       rx
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))));
       D1_data[i+1] = L_d0;
        /* symbol 4 */
```



```
= Enc2[i+1];
        d0
            = d0 - 0.5;
        rx = tx + SIGMA_24_4QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
                  (\exp(n*(rx+0.5)*(rx+0.5)));
        D2_parity[i+1] = L_d0;
D1_parity[i+1] = 0.0;
        D1_parity[i+1]
        D2_parity[i] = 0.0;
        i = i+1;
#endif
/*mio*/
#ifdef R26 4QAM
    * Channel: we transmit two 2-AM symbols to emulate a 4-QAM symbol.
     ^{\star} 2 info bits and 4 parity bits are mapped to 3 4-QAM symbols which in
     * turn are simulated as 6 2-AM symbols to achieve 1bit/s/Hz
     \mbox{*} INT_SIZE to be a multiple of 2
    n = (-1.0) / (2 * SIGMA 26 4QAM * SIGMA 26 4QAM);
    for (i = 0; i < INT_SIZE; i++)
      {
        /* symbol 1 */
        d0 = data[i];
            = d0 - 0.5;
        tx
        rx = tx + SIGMA_26_4QAM * gasdev();
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))));
        D1_data[i]
                     = L_d0;
        /* symbol 2 */
        d0 = Enc1[i];
        tx = d0 - 0.5;
           = tx + SIGMA_26_4QAM * gasdev();
        L d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))));
        D1 parity[i] = L d0;
        /* symbol 3 */
        d0 = Enc2[i];
        tx = d0 - 0.5;
            = tx + SIGMA_26_4QAM * gasdev();
        rx
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))));
        D2_parity[i] = L_d0;
        /* symbol 4 */
        d0 = data[i+1];
           = d0 - 0.5;
= tx + SIGMA_26_4QAM * gasdev();
        tx
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                   (exp(n*(rx+0.5)*(rx+0.5))));
        D1_data[i+1]
                       = L d0;
        /* symbol 5 */
            = Enc1[i+1];
            = d0 - 0.5;
        tx
            = tx + SIGMA 26 4QAM * gasdev();
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                   (exp(n*(rx+0.5)*(rx+0.5))));
        D1_parity[i+1] = L_d0;
        /* symbol 6 */
        d0
            = Enc2[i+1];
        tx = d0 - 0.5;
        rx = tx + SIGMA_26_4QAM * gasdev();
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                   (exp(n*(rx+0.5)*(rx+0.5))));
```



```
D2_parity[i+1] = L_d0;
       i = i+1;
#endif
/*mio*/
#ifdef R46_8QAM
    * I dimension:
     * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1):
            01----11
          -1.5 -0.5 0.5 1.5
     * Q dimension:
     * d0 is MSB in a 2-AM:(d0):
            0----1
          -0.5 0.5
     ^{\star} We transmit one 4A-M symbol and one 2-AM symbol to emulate a 32QAM symbol.
     * 4 info bits and 2 parity bits are mapped to 2 8QAM symbols.
     * INT_SIZE to be a multiple of 4
    for(i = 0; i < INT SIZE; i++)
        /* symbol 1: 4AM */
       d0 = data[i];
       d1 = Encl[i];
       tx = d0 - d1 + 2*d0*d1 - 0.5;
       rx = tx + SIGMA_4AM_of_46_8QAM * gasdev();
          = (-1.0) / (2 * SIGMA_4AM_of_46_8QAM * SIGMA_4AM of 46 8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                 (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
       L_dl = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                  (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1 data[i] = L d0;
       Dl_parity[i] = L_dl;
        /* symbol 2: 2AM */
       d0 = data[i+1];
       tx = d0 - 0.5;
          = tx + SIGMA_2AM_of 46 8QAM * gasdev();
          = (-1.0) / (2 * SIGMA 2AM of 46 8QAM * SIGMA 2AM of 46 8QAM);
       L d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                 (\exp(n*(rx+0.5)*(rx+0.5))));
       D1 data[i+1]
                    = L d0;
        /* symbol 3: 4AM */
       d0 = data[i+2];
       d1 = Enc2[i+2];
           = d0 - d1 + 2*d0*d1 - 0.5;
          = tx + SIGMA_4AM_of_46_8QAM * gasdev();
          = (-1.0) / (2 * SIGMA 4AM of 46 8QAM * SIGMA 4AM of 46 8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                 (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
       L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
                 (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1 data[i+2]
                     = L_d0;
       D2 parity[i+2] = L d1;
        /* symbol 2: 4AM */
       d0 = data[i+3];
       tx = d0 - 0.5;
       rx = tx + SIGMA_2AM_of_46_8QAM * gasdev();
       n = (-1.0) / (2 * SIGMA 2AM of 46 8QAM * SIGMA 2AM of 46 8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                 (\exp(n*(rx+0.5)*(rx+0.5))));
       D1_data[i+3] = L_d0;
   D1 parity[i+1]
                    = 0.0;
   D1 parity[i+2]
                    = 0.0;
```



```
D1_parity[i+3]
                    = 0.0;
   D2_parity[i] = 0.0;
   D2_parity[i+1]
                    = 0.0;
   D2_parity[i+3]
                    = 0.0;
       i = i+3;
#endif
/*mio*/
#ifdef R26_8QAM
   /*
    * I dimension:
    * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1):
            01----11
          -1.5 -0.5 0.5 1.5
    * Q dimension:
     * d0 is MSB in a 2-AM:(d0):
            0----1
          -0.5 0.5
    * We transmit one 4A-M symbol and one 2-AM symbol to emulate a 8QAM symbol.
     * 2 info bits and 4 parity bits are mapped to 2 8QAM symbols.
    * INT SIZE to be a multiple of 2
   for(i = 0; i < INT SIZE; i++)
    /* symbol 1: 4AM */
       d0 = data[i];
       d1 = Encl[i];
       tx
           = d0 - d1 + 2*d0*d1 - 0.5;
           = tx + SIGMA_4AM_of_26_8QAM * gasdev();
       rx
          = (-1.0) / (2 * SIGMA 4AM of 26 8QAM * SIGMA 4AM of 26 8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
       L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                 (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1 data[i] = L d0;
       D1_parity[i] = L_d1;
   /* symbol 2: 2AM */
       d0 = Enc2[i];
       tx = d0 - 0.5;
           = tx + SIGMA_2AM_of_26_8QAM * gasdev();
       n = (-1.0) / (2 * SIGMA_2AM_of_26_8QAM * SIGMA_2AM_of_26_8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                 (exp(n*(rx+0.5)*(rx+0.5))));
       D2_parity[i]
                     = L_d0;
       /* symbol 3: 4AM */
       d0 = Enc1[i+1];
       d1 = Enc2[i+1];
           = d0 - d1 + 2*d0*d1 - 0.5;
           = tx + SIGMA 4AM of 26 8QAM * gasdev();
          = (-1.0) / (2 * SIGMA_4AM_of_26_8QAM * SIGMA_4AM_of_26_8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) / 
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
       L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
                 (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1_parity[i+1] = L_d0;
       D2_parity[i+1] = L_d1;
   /* symbol 4: 2AM */
       d0 = data[i+1];
```

MPUTER PROGRAM LISTING APPENDIX

```
tx = d0 - 0.5;
       rx = tx + SIGMA 2AM_of_26_8QAM * gasdev();
       n = (-1.0) / (2 * SIGMA_2AM_of_26_8QAM * SIGMA_2AM_of_26_8QAM);
       L d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                 (\exp(n*(rx+0.5)*(rx+0.5))));
       D1 data[i+1]
                     = L_d0;
       i=\widetilde{i}+1;
#endif
/*mio*/
#ifdef R13_8QAM
    * I dimension:
     * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1):
           01----11
          -1.5 -0.5 0.5 1.5
    * Q dimension:
     * d0 is MSB in a 2-AM:(d0):
            0----1
          -0.5 0.5
    ^{\star} We transmit one 4A-M symbol and one 2-AM symbol to emulate a 8QAM symbol.
    * 1 info bits and 2 parity bits are mapped to 1 8QAM symbols.
    * INT_SIZE to be a multiple of 1
   for (i = 0; i < INT SIZE; i++)
   /* symbol 1: 4AM */
       d0 = data[i];
       d1 = Encl[i];
       tx = d0 - d1 + 2*d0*d1 - 0.5;
       rx = tx + SIGMA 4AM of 13 8QAM * gasdev();
       n = (-1.0) / (2 * SIGMA_4AM_of_13_8QAM * SIGMA_4AM_of_13_8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
       L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                  (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1_data[i] = L_d0;
       D1 parity[i] = L d1;
   /* symbol 2: 2AM */
       d0 = Enc2[i];
       tx = d0 - 0.5;

rx = tx + SIGMA_2AM_of_13_8QAM * gasdev();
       n = (-1.0) / (2 * SIGMA 2AM of 13 8QAM * SIGMA 2AM of 13 8QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))));
       D2_parity[i] = L_d0;
#endif
/*mio*/
#ifdef R412 16QAM
    * Channel: we transmit two 4-AM symbols to emulate a 16-QAM symbol.
    * 4 info bits and 8 parity bits are mapped to 3 16-QAM symbols which in
    * turn are simulated as 6\ 4\text{-AM} symbols to achieve 3bit/s/Hz
    * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1) = 01----00-|--10----11
                                                    -1.5 -0.5
                                                                0.5 1.5
    * INT_SIZE to be a multiple of 4
   n = (-1.0) / (2 * SIGMA_412_16QAM * SIGMA_412_16QAM);
   for (i = 0; i < INT_SIZE; i++)
```

OMPUTER PROGRAM LISTING APPOINT

```
/* symbol 1 */
d0 = data[i];
d1 = Enc1[i];
    = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
tx
     = tx + SIGMA 412 16QAM * gasdev();
L_d0 = log((exp(n^*(rx-1)*(rx-1))+exp(n^*(rx-3)*(rx-3))) /
          (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n^*(rx-1)^*(rx-1)) + \exp(n^*(rx+1)^*(rx+1))));
D1 data[i]
             = L_d0;
D1_parity[i] = L_d1;
/* symbol 2 */
d0
    = data[i+1];
     = Enc1(i+1);
d1
tx
    = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    = tx + SIGMA 412 16QAM * gasdev();
rx
L_d0 = log((exp(n^*(rx-1)*(rx-1))+exp(n^*(rx-3)*(rx-3))) /
          (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1))));
D1 data[i+1] = L d0;
D1_parity[i+1] = L_d1;
/* symbol 3 */
d0
    = Enc2[i];
d1
     = Enc2[i+1];
tx
    = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    = tx + SIGMA 412 16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n^*(rx+1)^*(rx+1))+\exp(n^*(rx+3)^*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n^*(rx-1)^*(rx-1))+\exp(n^*(rx+1)^*(rx+1))));
D2 parity[i] = L d0;
D2_parity[i+1] = L_d1;
/* symbol 4 */
d0
    = data[i+2];
    = Enc1[i+2];
    = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    = tx + SIGMA 412 16QAM * gasdev();
L d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n^*(rx+1)^*(rx+1))+\exp(n^*(rx+3)^*(rx+3))));
L d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1))));
D1_data[i+2] = L d0;
D1_parity[i+2] = L_d1;
  /* symbol 5 */
d0 = Enc2[i+2];
d1
    = Enc2[i+3];
    = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    = tx + SIGMA 412 16QAM * gasdev();
L_d0 = log((exp(n^*(rx-1)*(rx-1))+exp(n^*(rx-3)*(rx-3)))) /
          (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3)));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n^*(rx-1)^*(rx-1))+\exp(n^*(rx+1)^*(rx+1))));
D2_parity[i+2] = L_d0;
D2 parity[i+3] = L d1;
/* symbol 6 */
d0
    = data[i+3];
    = Encl[i+3];
d1
    = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    = tx + SIGMA 412 16QAM * gasdev();
L d0 = log((exp(n^{*}(rx-1)*(rx-1))+exp(n^{*}(rx-3)*(rx-3))))
          (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
          (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1)));
D1_data[i+3] = L_d0;
```



```
D1 parity[i+3] = L_d1;
               i = i+3;
#endif
/*mio*/
#ifdef R515 32QAM
   /*
    * I dimension:
      d0 is MSB and d2 is LSB in 8-AM: (d0, d1, d2):
            010---011---001---000---100---101---111---110
            -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
     * Q dimension:
     * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1):
            01----00----10----11
           -1.5 -0.5 0.5
    * We transmit one 8AM symbol and one 4AM symbol to emulate a 32QAM symbol.
     * 5 info bits and 10 parity bits are mapped to 3 32QAM symbols.
     * INT SIZE to be a multiple of 5
   for (i = 0; i < INT_SIZE; i++)
        /* symbol 1: 8AM */
   d0
      = data[i];
   d1 = Encl[i];
       d2 = Enc2[i];
       tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
       rx = tx + SIGMA_8AM_of_515_32QAM * gasdev();
       n = (-1.0) / (2 * SIGMA_8AM_of_515_32QAM_* SIGMA_8AM_of_515_32QAM);
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                  \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
       L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
       L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
   D1 data[i]
                  = L_d0;
   D1_parity[i]
                  = L_d1;
       D2 parity[i]
                     = L d2;
        /* symbol 2: 4AM */
       d0 = data[i+1];
       d1 = Encl[i+1];
           = d0 - d1 + 2*d0*d1 - 0.5;
          = tx + SIGMA 4AM of 515 32QAM * gasdev();
          = (-1.0) / (2 * SIGMA 4AM of 515 32QAM * SIGMA 4AM of 515 32QAM);
       L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
       L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
                  (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
       D1_data[i+1] = L d0;
       D2_parity[i+1] = L_d1;
       /* symbol 3: 8AM */
   d0
        = data[i+2];
        = Enc1[i+2];
   d1
       d2
           = Enc2[i+1];
           = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
       tx
       rx = tx + SIGMA_8AM_of_515_32QAM * gasdev();
```

COMPUTER PROGRAM LISTING AMENDIX

```
= (-1.0) / (2 * SIGMA 8AM of 515 32QAM * SIGMA 8AM of 515 32QAM);
      L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) + exp(n*(rx-1.5)) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                          exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));
      L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5))) +
                           \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
      L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5))) +
                          \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                         (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+2]
                          = L_d0;
D1_parity[i+2] = L_d1;
      D2 parity[i+1] = L d2;
       /* symbol 4: 4AM */
      d0 = data[i+3];
      d1 = Enc2[i+2];
      tx = d0 - d1 + 2*d0*d1 - 0.5;
            = tx + SIGMA 4AM_of_515_32QAM * gasdev();
             = (-1.0) / (2 * SIGMA_4AM_of_515_32QAM * SIGMA_4AM of 515 32QAM);
      L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
      L_dl = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                         (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
      D1_data[i+3] = L_d0;
      D2_parity[i+2] = L_d1;
       /* symbol 5: 8AM */
d0
       = data[i+4];
        = Encl[i+3];
      d2 = Enc2[i+3];
              = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
      rx = tx + SIGMA_8AM_of_515_32QAM * gasdev();
n = (-1.0) / (2 * SIGMA_8AM_of_515_32QAM * SIGMA_8AM_of_515_32QAM);
      L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)));
      L d1 = log((exp(n*(rx+3.5)*(rx+3.5))) + exp(n*(rx+2.5)*(rx+2.5)) +
                          \exp(n^*(rx-2.5)*(rx-2.5))+\exp(n^*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
      L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5))) +
                          \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                         (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+4]
                          = L d0;
D1_parity[i+3] = L_d1;
      D2 parity[i+3] = L d2;
       /* symbol 4: 4AM */
      d0 = Encl[i+4];
      dl = Enc2[i+4];
             = d0 - d1 + 2*d0*d1 - 0.5;
             = tx + SIGMA_4AM_of__515_32QAM * gasdev();
           = (-1.0) / (2 * SIGMA_4AM_of_515_32QAM * SIGMA_4AM_of_515_32QAM);
      L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5))));
     L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))) /
                         (\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx+0.5)*(rx+0.5))));
      D1 parity[i+4] = L d0;
      D2 parity[i+4] = L d1;
      i = i+4:
```



```
#endif
/*mio*/
#ifdef R26 64QAM
         * Channel:
         * d0 is MSB and d2 is LSB in 8AM: (d0,d1,d2):
                       010---011---001---000---100---101---111---110
                      -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
       /*
         * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
         \star 2 info bits and 4 parity bits are mapped to 1 64QAM symbols which in
         * turn are simulated as 2 8AM symbols to achieve 2bit/s/Hz.
         * INT_SIZE to be a multiple of 2
         */
             = (-1.0) / (2 * SIGMA_26_64QAM * SIGMA_26_64QAM);
       for (i = 0; i < INT SIZE; i++)
       /* symbol 1 */
             d0 = data(i);
       d1
             = Enc1[i];
             d2 = Enc2[i];
                      = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
               = tx + SIGMA_26_64QAM * gasdev();
             L d0 = \log((\exp(n^*(rx-0.5)^*(rx-0.5)) + \exp(n^*(rx-1.5)^*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
             L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));
             L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
       D1 data[i]
                                   = L d0;
       D1 parity[i]
                                   = L_d1;
             D2_parity[i] = L d2;
       /* symbol 2 */
             d0
                      = data[i+1];
       d1
               = Enc1[i+1];
             d2
                    = Enc2[i+1];
                     = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
               = tx + SIGMA 26 64QAM * gasdev();
             L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
             L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
             L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
       D1 data[i+1]
                                       = L d0;
       D1 parity[i+1]
                                       = L_d1;
       D2_parity[i+1]
                                       = L_d2;
             i = i+1;
```



```
#endif
/*mio*/
#ifdef R36_64QAM
          /*
            * Channel:
                  d0 is MSB and d2 is LSB in 8AM: (d0,d1,d2):
                                   010---011---001---000---100---101---111---110
                                 -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
             * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
             \star 6 info bits and 6 parity bits are mapped to 2 64QAM symbols which in
             * turn are simulated as 4 8AM symbols to achieve 2bit/s/Hz.
             * INT SIZE to be a multiple of 6
            */
                  = (-1.0) / (2 * SIGMA_36_64QAM * SIGMA_36_64QAM);
          for (i = 0; i < INT_SIZE; i++)
          /* symbol 1 */
                   d0 = data[i];
          d1 = data[i+1];
                   d2 = Encl[i];
                               = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
                       = tx + SIGMA_36_64QAM * gasdev();
                   L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5)*(rx-1.5)) +
                                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))/
                                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
                   L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                                                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
                   L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                                    \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
          D1 data[i]
                                                   = L d0;
          D1 data[i+1]
                                                   = L_d1;
                   D1 parity[i] = L d2;
          /* symbol 2 */
                   d0
                                = data[i+2];
                       = Enc1[i+2];
                   d2
                             = Enc2[i+1]:
                                = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
                      = tx + SIGMA 36 64QAM * gasdev();
                   L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
                   L dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
                   L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
          D1_data[i+2]
                                                         = L d0;
          D1 parity[i+2]
                                                         = L d1;
          D2_parity[i+1]
                                                        = L_d2;
```

```
/* symbol 3 */
       d0 = data[i+3];
       = data[i+4];
       d2 = Enc2[i+3];
       tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
        = tx + SIGMA_36_64QAM * gasdev();
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))/
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
       L dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
       L d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)));
    D1 data[i+3]
                     = L_d0;
                     = L_d1;
    D1 data[i+4]
       D2_parity[i+3]
                        = L_d2;
    /* symbol 2 */
            = data[i+5];
       d0
    d1
        = Encl[i+4];
       d2
           = Enc2[i+5];
       tx
           = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
        = tx + SIGMA_36_64QAM * gasdev();
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
       L_dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5))) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
       L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n^*(rx-1.5)*(rx-1.5))+\exp(n^*(rx-2.5)*(rx-2.5)))
                  (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
    D1 data[i+5]
                     = L_d0;
   D1_parity[i+4]
                     = L_d1;
    D2_parity[i+5]
                     = L d2;
    D2_parity[i]
                     = 0.0;
    D1 parity[i+1]
                     = 0.0;
    D2_parity[i+2]
                     = 0.0;
                     = 0.0;
   D1 parity[i+3]
                     = 0.0;
    D2 parity[i+4]
    D1_parity[i+5]
                     = 0.0:
       i = i+5;
#endif
/*mio*/
#ifdef R721_128QAM
    * Q dimension:
      d0 is MSB and d2 is LSB in 8-AM:(d0,d1,d2):
            010---011---001---000---100---101---111---110
            -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
     * I dimension:
     * d0 is MSB and d3 is LSB in 16AM: (d0.d1.d2.d3):
             0010---0011---0001---0000---0100---0101---0111---0110
             -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
```

```
1010---1011---1001---1000---1100---1101---1111---1110
                              6.5
                                          5.5
                                                     4.5
                                                                   3.5 2.5
                                                                                        1.5
    INT_SIZE to be a multiple of 7
for (i = 0; i < INT_SIZE; i++)
   {
      /* symbol 1 Q dimension: 8AM */
      d0 = data[i+2];
d1 = Enc1[i+1];
      d2 = Enc2[i+1];
      tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
      rx = tx + SIGMA_8AM_of_721_128QAM * gasdev();
     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
     L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))/
                         (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
      L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))/
                         (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+2]
                             = L d0;
D1 parity[i+1]
                              = L_d1;
      D2_parity[i+1]
                                   = L d2;
/* symbol 2 I dimension: 16AM */
     d0 = data[i];
d1 = data[i+1];
d2 = Enc1[i];
      d3 = Enc2[i];
     tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
      tx = (d0 == 0 ? (tx - 4): (4 - tx));
     rx = tx + SIGMA_16AM_of_721_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_721_128QAM * SIGMA_16AM_of_721_128QAM);
      L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                          \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                          \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                          \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                          \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
     L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                          \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                          \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                          exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                          \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
     L d2 = \log((\exp(n*(rx+7.5)*(rx+7.5))) + \exp(n*(rx+6.5)*(rx+6.5)) +
                          \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                          \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                         (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                          \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
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\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
      L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                          \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                          \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                         (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                          \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                          \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1_data[i]
                          = L d0;
D1 data[i+1]
                          = L_d1;
      D1_parity[i]
                                = L_d2;
      D2 parity[i]
                                = L d3;
/* symbol 3 Q dimension: 8AM */
      d0 = data[i+4];
d1 = Encl[i+4];
      d2 = Enc2[i+3];
      tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA 8AM of 721 128QAM * gasdev();
           = (-1.0) / (2 * SIGMA_8AM_of_721_128QAM * SIGMA_8AM_of_721_128QAM);
      L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))/
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
     L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                         (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
     L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                         (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+4]
                             = L_d0;
D1_parity[i+4]
                             = L_d1;
      D2_parity[i+3]
                                   = L_d2;
/* symbol 4 I dimension: 16AM */
     d0 = data[i+3];
d1 = Enc1[i+3];
d2 = Enc1[i+2];
     d3 = Enc2[i+2];
      tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
      tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA 16AM of 721 128QAM * gasdev();
     n = (-1.0) / (2 * SIGMA_16AM_of_721_128QAM * SIGMA_16AM_of_721_128QAM);
     L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                          \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                          \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                         (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                          \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                          \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                          \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
     L_dl = log((exp(n*(rx+3.5)*(rx+3.5))) + exp(n*(rx+2.5)*(rx+2.5)) +
                          \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                          \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                          \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                        (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                          \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                          \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                          \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
     L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
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\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                         \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                         \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                        (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                         \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                         \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                         \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
     L d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                         \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                         \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                         \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                        (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                         \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                         \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))+
                         \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5)));
D1 data[i+3]
                             = L d0;
D1_parity[i+3]
                            = L_d1;
     D1 parity[i+2]
                                   = L_d2;
                                   = L_d3;
      D2_parity[i+2]
/* symbol 5 Q dimension: 8AM */
     d0 = data[i+6];
d1 = Enc1[i+6];
     d2 = Enc2[i+6];
     tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
     = tx + SIGMA_8AM_of_721_128QAM * gasdev();
     n = (-1.0) / (2 * SIGMA 8AM of 721 128QAM * SIGMA 8AM of 721 128QAM);
     L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                         \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                        (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                         \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
     L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                         \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                      (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                         \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
     L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                         \exp(n^*(rx-1.5)*(rx-1.5)) + \exp(n^*(rx-2.5)*(rx-2.5)))
                        (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                         \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+6]
                             = L_d0;
D1_parity[i+6]
                            = L_d1;
     D2_parity[i+6]
                                  = L_d2;
/* symbol 6 I dimension: 16AM */
     d0 = data[i+5];
d1 = Encl[i+5];
d2 = Enc2[i+5];
     d3 = Enc2[i+4];
     tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
     tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_16AM_of_721_128QAM * gasdev();
     n = (-1.0) / (2 * SIGMA 16AM of 721 128QAM * SIGMA 16AM of 721 128QAM);
     L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                         \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                         \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                         \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                        (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                         \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                         \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                         \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
     L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                         \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                         \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                         \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
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(\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                  \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));
       L d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                  \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                  \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
       L d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                  \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                 (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                  \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
   D1 data[i+5]
                    = L d0;
   D1 parity[i+5]
                   = L d1;
       D2 parity[i+5]
                       = L d2;
       D2 parity[i+4]
                       = L_d3;
       i = i+6;
#endif
/*mio*/
#ifdef R824 256QAM
   /*
    * Channel:
    * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
            ^{\star} Channel: we transmit two 16AM symbols to emulate a 256QAM symbol.
    * 8 info bits and 16 parity bits are mapped to 3 256QAM symbols which in
    * turn are simulated as 6 16AM symbols to achieve 8/3bit/s/Hz.
    * INT_SIZE to be a multiple of 8
      = (-1.0) / (2 * SIGMA_824_256QAM * SIGMA_824_256QAM);
    * deinterleave data:
    */
   for (i = 0; i < INT SIZE; i++)
     data d[i] = data[i];
   r_deileava(data_d, rule);
   for(i = 0; i < INT_SIZE; i++)
       /* symbol 1 */
   d0 = data_d[i];
   d1 = data d[i+1];
   d2 = Encl[i];
       d3 = Enc2[i];
       tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
       tx = (d0 == 0 ? (tx - 4): (4 - tx));
       /* Test the mapping to the 16AM constellation:
       * if (i < 500)
```

```
printf("\n(%d%d%d%d) = %f", (int)d0, (int)d1, (int)d2, (int)d3, tx);
           */
rx
           = tx + SIGMA 58 256QAM * gasdev();
        L_{d0} = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
        L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
        L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                                 (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                                   \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
        L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) + exp(n*(rx+6.5)) + 
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                                 (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                                   \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1 data[i]
                                  = L d0;
D1_data(i+1)
                                  = L_d1;
        D1 parity[i]
                                           = L d2;
        D2_parity[i]
                                           = L_d3;
         /* symbol 2 */
d0 = data_d[i+2];
d1 = Enc1[i+2];
        d2 = Enc1[i+1];
        d3 = Enc2[i+1];
        tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
        tx = (d0 == 0 ? (tx - 4): (4 - tx));
          = tx + SIGMA 824_256QAM * gasdev();
        L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                                (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                  \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
        L dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5))) + exp(n*(rx+2.5)) +
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                                  \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
       L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5))) +
```

```
\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
               (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
   L d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
               (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5)));
D1 data[i+2]
                = L d0;
D1 parity[i+2] = L_d1;
D1_parity[i+1] = L_d2;
D2 parity[i+1] = L d3;
    /* symbol 3 */
d0
    = data d[i+3];
d1
     = Encl[i+3];
d2
     = Enc2[i+3];
   d3 = Enc1[i+2];
   tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
   tx = (d0 == 0 ? (tx - 4): (4 - tx));
= tx + SIGMA_{824}_{256QAM} * gasdev();
   L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
               (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
   L_dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
               (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
   L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
               (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
   L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
               (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1 data[i+3]
                 = L d0;
D1_parity[i+3]
                 = L_d1;
D2_parity[i+3]
                 = L_d2;
   D2 parity[i+2]
                     = L d3;
/* symbol 4 */
   = data d[i+4];
```



```
d1
    = data d[i+5];
   d2
        = Enc1(i+4);
   d3
        = Enc2[i+4];
   tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
   tx = (d0 == 0 ? (tx - 4) : (4 - tx));
    = tx + SIGMA_824_256QAM * gasdev();
   L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
              (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
               \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
   L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
               (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
   L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
              (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5))
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
   L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5))) + (rx+6.5))
               \exp(n^*(rx+1.5)*(rx+1.5))+\exp(n^*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
              (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1 data[i+4]
               = L d0;
D1_data[i+5]
               = L_d1;
   D1 parity[i+4] = L d2;
   D2 parity[i+4] = L d3;
   /* symbol 5 */
   d0
        = data_d[i+6];
     = Enc1[i+6];
     = Enc1[i+5];
   d3
        = Enc2[i+5];
   tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
   tx = (d0 == 0 ? (tx - 4): (4 - tx));
    = tx + SIGMA_824_256QAM * gasdev();
   L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) + r
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
              (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
               \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
   L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
              (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
```



```
\exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
   L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
               (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
   L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
               (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1 data[i+6]
                 = L d0;
D1_parity[i+6]
                 = L d1;
D1_parity[i+5]
                 = L_d2;
                    = L d3;
   D2_parity[i+5]
/* symbol 4 */
    = data d[i+7];
d0
     = Enc1[i+7];
   d2
        = Enc2[i+7];
   d3
        = Enc2[i+6];
   tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
   tx = (d0 == 0 ? (tx - 4): (4 - tx));
     = tx + SIGMA 824 256QAM * gasdev();
   L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
              (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
               \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));
   L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
               (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
               exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
   L d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n^*(rx-0.5)^*(rx-0.5)) + \exp(n^*(rx-1.5)^*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
              (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
   L d3 = \log((\exp(n*(rx+5.5)*(rx+5.5))) + \exp(n*(rx+6.5)*(rx+6.5)) +
               \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
              (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
               exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1 data[i+7]
               = L_d0;
D1 parity[i+7]
                 = L_d1;
   D2_parity[i+7] = L_d2;
   D2 parity[i+6] = L d3;
```



```
i = i+7;
            interleave data:
       r_ileav(D1_data, rule);
#endif
/*mio*/
#ifdef R69 512QAM
         * Interleaver should be a multiple of 3, e.g., 6144
         * Q dimension:
         * d0 is MSB and d4 is LSB in 32AM: (d0,d1,d2,d3,d4):
                         00010 -- 00011 -- 00001 -- 00000 -- 00100 -- 00101 -- 00111 -- 00110 \\
                         -15.5 -14.5 -13.5 -12.5 -11.5 -10.5 -9.5
                         01010 -- 01011 -- 01001 -- 01000 -- 01100 -- 01101 -- 01111 -- 01110 \\
                         -0.5 -1.5 -2.5 -3.5 -4.5 -5.5 -6.5
                         11010--11011--11001--11000--11100--11101--11111--11110
                                    1.5
                                                 2.5
                                                              3.5
                                                                            4.5
                                                                                          5.5
                                                                                                           6.5
                         10010--10011--10001--10000--10100--10101--10111--10110
                         15.5 14.5 13.5 12.5 11.5 10.5 9.5
          * I dimension:
         * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
                         \tt 0010---0011---0001---0000---0100---0101---0111---0110
                         -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5
                         1010---1011---1001---1000---1100---1101---1111---1110
                                    6.5
                                                  5.5 4.5 3.5 2.5 1.5
         */
         * deinterleave data:
         */
       for (i = 0; i < INT SIZE; i++)
           data d(i) = data[i];
       r_deileava(data_d, rule);
       for(i = 0; i < INT_SIZE; i++)
          {
       /* symbol 1, Q dimension: 32AM */
       d0 = data_d[i];
       d1 = data d[i+1];
              d2 = Enc1[i];
              d3 = Enc2[i];
              d4 = Enc1[i+1];
              tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
              tx = (d1 == 0 ? (tx - 4): (4 - tx));
              tx = (d0 == 0 ? (tx - 8): (8 - tx));
       rx = tx + SIGMA 32AM of 39 512QAM * gasdev();
              n = (-1.0) / (2 * SIGMA_32AM_of_39_512QAM * SIGMA_32AM_of_39_512QAM);
              L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                    \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                                     \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                                     \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                                     \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                                     exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
                                   (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                    \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                     exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                                    \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                                    \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
```

```
\exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                  \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                  \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)));
L d1 = \log((\exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5))*(rx-1.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                  \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                  \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                  \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
                 (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                  \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                  \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                  \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
                  exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
                  exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
                  \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                  \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                  \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                  \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                  \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                  \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)))
                 (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                  \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                  \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                  \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                  \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5))));
L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) + exp(n*(rx+1.5)) + 
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                  \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                  \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                  \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                  \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
                 (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                  \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                  \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                  \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5))) + (rx+1.5)
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                  \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                  \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-13.5)*(rx-13.5)))
                 (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                  \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
                  \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                  \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
                  \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-15.5)*(rx-15.5)));
```

COMPUTER PROGRAM LISTING APPOINT

```
D1_data[i]
                   = L_d0;
    D1_data[i+1]
                   = L_d1;
       D1_parity[i] = L_d2;
                     = L_d3;
       D2_parity[i]
       Dl_parity[i+1] = L_d4;
        /* symbol 1, I dimension: 16AM */
    d0 = data_d[i+2];
    d1 = Encl[i+2];
   d2 = Enc2[i+2];
       d3 = Enc2[i+1];
       tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
       tx = (d0 == 0 ? (tx - 4): (4 - tx));
    rx = tx + SIGMA 16AM of 39 512QAM * gasdev();
       n = (-1.0) / (2 * SIGMA_16AM_of_39_512QAM * SIGMA_16AM_of_39_512QAM);
       L_{d0} = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
       L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
       L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                   \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)));
       L d3 = \log((\exp(n*(rx+5.5)*(rx+5.5))) + \exp(n*(rx+6.5)*(rx+6.5)) +
                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                  (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                   \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
                  = L d0;
    D1_data[i+2]
    D1_parity[i+2] = L_d1;
       D2 parity[i+2] = L d2;
       D2 parity[i+1] = L d3;
       i = i+2;
     }
      interleave data:
    r_ileav(D1 data, rule);
#endif
/*mio*/
#ifdef R12_16QAM
     * Channel: we transmit two 4-AM symbols to emulate a 16-QAM symbol.
```

```
^{\star} 2 info bits and 2 parity bits are mapped to 1 16-QAM symbols which in
     * turn are simulated as 2 4-AM symbols to achieve 2bit/s/Hz
     * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1) = 01--00-|-10--11
                                                       -3 -1
     * INT_SIZE to be a multiple of 2
    n = (-1.0) / (2 * SIGMA_12_16QAM * SIGMA_12_16QAM);
    for (i = 0; i < INT SIZE; i++)
        /* symbol 1 */
        d0 = data[i];
        d1 = Enc1[i];
        tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;

rx = tx + SIGMA_{12_{16QAM}} * gasdev();
        L d0 = log((exp(n^*(rx-1)*(rx-1))+exp(n^*(rx-3)*(rx-3))) /
                   (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3)));
        L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
                   (\exp(n^*(rx-1)^*(rx-1))+\exp(n^*(rx+1)^*(rx+1)));
        D1 data[i]
                     = L_d0;
        D1_parity[i] = L_d1;
        D2_parity[i] = 0.0;
        /* symbol 2 */
        d0
            = data[i+1];
             = Enc2[i+1];
        d1
        tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
            = tx + SIGMA 12 16QAM * gasdev();
        L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
                   (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3))));
        L d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
                   (\exp(n^*(rx-1)^*(rx-1))+\exp(n^*(rx+1)^*(rx+1))));
        D1_data[i+1] = L_d0;
        D2 parity[i+1] = L d1;
        D1 parity[i+1] = 0.0;
        i = i+1;
      }
#endif
#ifdef R34 16QAM
     ^{\star} Channel: we transmit two 4-AM symbols to emulate a 16-QAM symbol.
     * 6 info bits and 2 parity bits are mapped to 2 16-QAM symbols which in
     * turn are simulated as 4 4-AM symbols to achieve 3bit/s/Hz * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1) = 01--00-|-10--11
                                                       -3 -1
     * INT_SIZE to be a multiple of 6
    */
    n = (-1.0) / (2 * SIGMA_34_16QAM * SIGMA_34_16QAM);
    for (i = 0; i < INT_SIZE; i++)
      {
        /* symbol 1 */
        d0 = data[i];
        d1 = data[i+1];
        tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
        rx = tx + SIGMA_34_16QAM * gasdev();
        L d0 = log((exp(n^*(rx-1)^*(rx-1))+exp(n^*(rx-3)^*(rx-3))) /
                   (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3))));
        L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
                   (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1)));
        D1 data[i] = L d0;
        D1_data[i+1] = L_d1;
        /* symbol 2 */
            = data[i+2];
        dl = Encl[i+1];
        tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;

rx = tx + SIGMA_34_16QAM * gasdev();
        L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3)))) /
```



```
(\exp(n^*(rx+1)^*(rx+1)) + \exp(n^*(rx+3)^*(rx+3))));
        L d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
                  (\exp(n^*(rx-1)^*(rx-1)) + \exp(n^*(rx+1)^*(rx+1))));
        D1 data[i+2] = L_d0;
        D1_parity[i+1] = L_d1;
        /* symbol 3 */
            = data[i+3];
        40
            = data[i+4];
            = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
        t.x
            = tx + SIGMA_34_16QAM * gasdev();
        L_d0 = log((exp(n^*(rx-1)*(rx-1))+exp(n^*(rx-3)*(rx-3))) /
                  (\exp(n^*(rx+1)^*(rx+1))+\exp(n^*(rx+3)^*(rx+3))));
        L d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))))
                  (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1))));
        D1 data[i+3] = L_d0;
        D1_{data[i+4]} = L_{dl}
        /* symbol 4 */
        d0
            = data[i+5];
        d1
             = Enc2[i+4];
            = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
        t.x
            = tx + SIGMA 34 16QAM * gasdev();
        L_{d0} = log((exp(n^{*}(rx-1)*(rx-1))+exp(n^{*}(rx-3)*(rx-3)))) /
                  (\exp(n*(rx+1)*(rx+1))+\exp(n*(rx+3)*(rx+3))));
        L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3)))) /
                  (\exp(n*(rx-1)*(rx-1))+\exp(n*(rx+1)*(rx+1))));
                      = L d0;
        D1 data[i+5]
        D2_parity[i+4] = L_d1;
        D1 parity[i]
                       = 0.0;
        D1_parity[i+2] = 0.0;
        D1_parity[i+3] = 0.0;
        D1_parity[i+4] = 0.0;
        D1_parity[i+5] = 0.0;
        D2 parity[i]
                      = 0.0;
        D2 parity[i+1] = 0.0;
        D2 parity[i+2] = 0.0;
        D2_parity[i+3] = 0.0;
        D2 parity[i+5] = 0.0;
        i = i+5;
#endif
#ifdef R56 64QAM
      d0 is MSB and d2 is LSB in 8AM: (d0,d1,d2):
            */
    /*
    * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
     ^{\star} 10 info bits and 2 parity bits are mapped to 2 64QAM symbols which in
     * turn are simulated as 4 8AM symbols to achieve 5bit/s/Hz.
     * INT_SIZE to be a multiple of 10
   n = (-1.0) / (2 * SIGMA_56_64QAM * SIGMA_56_64QAM);
    for (i = 0; i < INT SIZE; i++)
        /* symbol 1 */
        d0 = data[i];
        d1 = data[i+1];
       d2 = Encl[i];
       tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1)) < 0?(d2-0.5) : (0.5-d2));
            = tx + SIGMA_56_64QAM * gasdev();
       L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))/
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
```



```
L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
           (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
           (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
                = L_d0;
D1_data[i]
D1 data[i+1]
                = L d1;
               = L_d2;
D1_parity[i]
D1_parity[i+1] = 0;
               = 0:
D2_parity[i]
D2_parity[i+1] = 0;
 /* symbol 2 */
d0
     = data[i+2];
     = data[i+3];
d1
     = data[i+4];
     = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    = tx + SIGMA_56_64QAM * gasdev();
L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5))) + exp(n*(rx+2.5))*(rx+2.5))
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
           (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
           (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+2]
               = L d0;
D1_data[i+3]
                = L_d1;
D1_data[i+4]
               = L_d2;
D1_parity[i+2] = 0;
D1_parity[i+3] = 0;
D1_parity[i+4] = 0;
D2_parity[i+2] = 0;
D2 parity[i+3] = 0;
D2_parity[i+4] = 0;
/* symbol 3 */
d0
     = data[i+5];
     = data[i+6];
     = Enc2[i+5];
d2
     = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
     = tx + SIGMA_56_64QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))/
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5))));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
           (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5))) + exp(n*(rx+1.5)*(rx+1.5))
            \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
           (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
D1 data[i+5]
               = L_d0;
D1_data[i+6]
               = L_d1;
D2_parity[i+5] = L_d2;
D2_parity[i+6] = 0;
D1 parity[i+5] = 0;
```

OMPUTER PROGRAM LISTING APPLICATION

```
D1 parity[i+6] = 0;
                /* symbol 4 */
                         = data[i+7];
               d0
                          = data[i+8];
               d1
                        = data[i+9];
                        = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
                       = tx + SIGMA 56 64QAM * gasdev();
              L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                    (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)));
              L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                    (\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5))));
              L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                     \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))
                                    (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
               D1 data[i+7]
                                           = L_d0;
               D1_data[i+8]
                                           = L_d1;
              D1 data[i+9]
                                           = L d2;
              D1_parity[i+7] = 0;
              D1_parity[i+8] = 0;
              D1_parity[i+9] = 0;
              D2_parity[i+7] = 0;
              D2 parity[i+8] = 0;
              D2_parity[i+9] = 0;
              i = i+9;
#endif
#ifdef R57_128QAM
         * Q dimension:
          * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
                       * I dimension:
          * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
                         0010---0011---0001---0000---0100---0101---0111---0110
                         -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
                         1010---1011---1001---1000---1100---1101---1111---1110
                                         6.5
                                                      5.5
                                                                    4.5
                                                                                  3.5
                                                                                             2.5
                                                                                                          1.5
         * INT_SIZE to be a multiple of 5
       for (i = 0; i < INT SIZE; i++)
               /* Q dimension: 8AM */
               d0 = data[i];
               dl = data[i+1];
              d2 = Encl[i];
              tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
              rx = tx + SIGMA_8AM_of_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_8AM_of_128QAM * SIGMA_8AM_of_128QAM);
              L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                    (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                     exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));
              L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
```



```
(\exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)));
L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx-1.5)*(rx-1.5))+\exp(n*(rx-2.5)*(rx-2.5)))/
                   (\exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5))));
 D1_data[i]
                            = L d0;
 D1 data[i+1]
                            = L d1;
D1_parity[i]
                           = L_d2;
D1 parity[i+1] = 0.0;
D1_parity[i+2] = 0.0;
D1 parity[i+3] = 0.0;
D1 parity[i+4] = 0.0;
 /* I dimension: 16AM */
 d0 = data[i+2];
 d1 = data[i+3];
 d2 = data[i+4];
d3 = Enc2[i];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA 16AM of 128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_128QAM * SIGMA_16AM_of_128QAM);
L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                     \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                   (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                     exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                     \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                     \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                   (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                    \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                    \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                    \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                    \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                   (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                    \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                    \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
L d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                    \exp(n^*(rx+1.5)*(rx+1.5))+\exp(n^*(rx+2.5)*(rx+2.5)) +
                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                    \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                   (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                    \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                    \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
 D1 data[i+2]
                           = L_d0;
 D1 data[i+3]
                           = L_d1;
D1_data[i+4]
                          = L d2;
                          = L d3;
D2_parity[i]
D2 parity[i+1] = 0.0;
D2 parity[i+2] = 0.0;
D2 parity[i+3] = 0.0;
D2_parity[i+4] = 0.0;
i = i+4;
```

#endif



```
#ifdef R58_256QAM
   /*
    * Channel:
      d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
            0010---0011---0001---0000---0100---0101---0111---0110
                  -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
             1010---1011---1001---1000---1100---1101---1111---1110
                    6.5
                         5.5
                                   4.5
                                          3.5 2.5 1.5
    * Channel: we transmit two 16AM symbols to emulate a 256QAM symbol.
    * 10 info bits and 6 parity bits are mapped to 2 256QAM symbols which in
    * turn are simulated as 4 16AM symbols to achieve 6bit/s/Hz.
    * INT_SIZE to be a multiple of 10
       = (-1.0) / (2 * SIGMA 58 256QAM * SIGMA 58 256QAM);
    * deinterleave data:
    */
   for (i = 0; i < INT SIZE; i++)
     data d(i) = data[i];
   r_deileava(data d, rule);
   for(i = 0; i < INT SIZE; i++)
       /* symbol 1 */
       d0 = data_d[i];
       d1 = data d[i+1];
       d2 = data d[i+2];
       d3 = Encl[i];
       tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
       tx = (d0 == 0 ? (tx - 4): (4 - tx));
       /* Test the mapping to the 16AM constellation:
        * if (i < 500)
        * printf("\n(%d%d%d%d) = %f", (int)d0, (int)d1, (int)d2, (int)d3, tx);
        */
            = tx + SIGMA_58_256QAM * gasdev();
       L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5))) + \exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                  \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
       L_dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                  \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                  \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
       L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                  \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                  \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
```



```
L d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                     \exp(n^*(rx+1.5)^*(rx+1.5)) + \exp(n^*(rx+2.5)^*(rx+2.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                     exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
                    (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                     \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                     \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
 D1_data[i]
                            = L_d0;
 D1 data[i+1]
                            = L d1;
D1 data[i+2]
                           = Ld2;
D1_parity[i]
                           = L_d3;
D1_parity[i+1] = 0;
D1_parity[i+2] = 0;
D2 parity[i]
                          = 0;
D2_parity[i+1] = 0;
 /* symbol 2 */
 d0 = data d[i+3];
dl = data d[i+4];
d2 = Enc2[i+2];
d3 = Enc1[i+4];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));

rx = tx + SIGMA 58 256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                     \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                    (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                     \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                     \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                     \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                     \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                    (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                     \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                     \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
L d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                     \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                    (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                     \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                     \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)));
L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) + exp(n*(rx+6.5)) + 
                     \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                     \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                    \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                    (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                     \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                     \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
 D1 data[i+3]
                           = L_d0;
 D1_data[i+4]
                           = L d1;
 D2_parity[i+2] = L_d2;
 D1 parity[i+4] = L d3;
D1_parity[i+3] = 0;
D2_parity[i+3] = 0;
D2 parity[i+4] = 0;
 /* symbol 3 */
        = data d[i+5];
```



```
= data_d[i+6];
d1
     = data d[i+7];
d2
     = Enc2[i+5];
d3
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
     = tx + SIGMA_58_256QAM * gasdev();
L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5)*(rx-1.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
           (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
           (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
            exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
L d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
           (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
            \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5)));
D1_data[i+5]
                = L d0;
D1 data[i+6]
                = L d1;
D1_data[i+7]
                = L_d2;
D2 parity[i+5] = L d3;
D2_parity[i+6] = 0;
D2_parity[i+7] = 0;
D1 parity[i+5] = 0;
D1_parity[i+6] = 0;
/* symbol 4 */
d0
     = data_d[i+8];
     = data d[i+9];
d1
d2
     = Encl[i+7];
     = Enc2[i+9];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_58_256QAM * gasdev();
L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
           (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L dl = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
```

OMPUTER PROGRAM LISTING APPLICIX

```
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
                                      \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                                      exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                                      \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
              L d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                                      \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                      \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                                    (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                                      \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                                      \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                      \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
              L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) + exp(n*(rx+6.5)) + 
                                      \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                                      exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                     \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                                    (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                                     \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                     \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                     \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
                D1 data[i+8]
                                           = L d0;
                                           = L_d1;
               D1_data[i+9]
               D1 parity[i+7] = L d2;
               D2 parity[i+9] = L d3;
              D1_parity[i+8] = 0;
              D1_parity[i+9] = 0;
              D2 parity[i+7] = 0;
              D2 parity[i+8] = 0;
              i = i+9;
             interleave data:
       r_ileav(D1_data, rule);
#endif
#ifdef R68_256QAM
             Channel:
          * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
                         \tt 0010---0011---0001---0000---0100---0101---0111---0110
                         -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
                         1010---1011---1001---1000---1100---1101---1111---1110\\
                                      6.5
                                                   5.5
                                                                 4.5
                                                                                3.5
                                                                                               2.5
                                                                                                            1.5
         ^{\star} Channel: we transmit two 16AM symbols to emulate a 256QAM symbol.
         ^{\star} 6 info bits and 2 parity bits are mapped to one 256QAM symbol which in
         * turn is simulated as 2 16AM symbols to achieve 6bit/s/Hz.
         * INT_SIZE to be a multiple of 6
               = (-1.0) / (2 * SIGMA_68_256QAM * SIGMA_68_256QAM);
         * deinterleave data:
         */
       for (i = 0; i < INT SIZE; i++)
           data d[i] = data[i];
       r deileava(data d, rule);
       for(i = 0; i < INT_SIZE; i++)
               /* symbol 1 */
               d0 = data d[i];
               d1 = data_d[i+1];
```



```
d2 = data_d[i+2];
 d3 = Encl[i];
 tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
 tx = (d0 == 0 ? (tx - 4): (4 - tx));
           = tx + SIGMA 68 256QAM * gasdev();
 L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                          (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                             \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                             \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
 L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) + exp(n*(rx+2.5)) + 
                            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                          (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                             \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
 L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                             \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                          (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                            \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                             \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                          (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                            \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
 D1 data[i]
                                     = L d0;
 D1 data[i+1]
                                    = L d1;
                                    = L_d2;
 D1 data[i+2]
 D1 parity[i]
                                    = L d3;
D1_parity[i+1] = 0;
 D1 parity[i+2] = 0;
 D2_parity[i]
                                   = 0:
D2_parity[i+1] = 0;
D2_parity[i+2] = 0;
  /* symbol 2 */
 d0 = data_d[i+3];
 dl = data_d[i+4];
d2 = data_d[i+5];
d3 = Enc2[i+3];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
              = tx + SIGMA_68_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                          (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                           \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                           exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
```

COMPUTER PROGRAM LISTING APPLICATION

```
\exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                  \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                  \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
       L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                  \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5))+
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                  \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
       L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                  \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                  \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                  \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                  (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                  \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                  \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                  \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
                      = L_d0;
       D1_data[i+3]
       D1 data[i+4]
                      = L_d1;
                     = L_d2;
       D1,data[i+5]
       D2_parity(i+3) = L_d3;
       D2 parity[i+4] = 0;
       D2 parity[i+5] = 0;
       D1_parity[i+3] = 0;
       D1_parity[i+4] = 0;
       D1 parity[i+5] = 0;
       i = i+5;
      interleave data:
   r ileav(D1 data, rule);
#endif
#ifdef R69_512QAM
    \star Interleaver should be a multiple of 12, e.g., 6144
    * Q dimension:
    * d0 is MSB and d4 is LSB in 32AM: (d0,d1,d2,d3,d4):
            \tt 00010--00011--00001--00000--00100--00101--00111--00110
            -15.5 -14.5 -13.5 -12.5 -11.5 -10.5 -9.5 -8.5
            \tt 01010--01011--01001--01000--01100--01101--01111--01110
                  -1.5 -2.5 -3.5 -4.5 -5.5 -6.5
            11010--11011--11001--11000--11100--11101--11111--11110
            0.5
                   1.5
                         2.5
                                 3.5
                                      4.5
                                              5.5
                                                      6.5
            10010--10011--10001--10000--10100--10101--10111--10110
            15.5 14.5 13.5 12.5 11.5 10.5 9.5
    * I dimension:
      d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
            0010---0011---0001---0000---0100---0101---0110
            -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
            1010---1011---1001---1000---1100---1101---1111---1110
                  6.5 5.5 4.5 3.5 2.5 1.5 0.5
```

```
*/
      deinterleave data:
for(i = 0; i < INT SIZE; i++)
    data d[i] = data[i];
r_deileava(data_d, rule);
for(i = 0; i < INT_SIZE; i++)
                symbol 1, Q dimension: 32AM */
         d0
               = data_d[i];
        d1
                 = data_d[i+1];
        d2
               = data_d[i+2];
               = data d[i+3];
        d4
               = Enc1[i];
        tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
       tx = (d1 == 0 ? (tx - 4): (4 - tx));
        tx = (d0 == 0 ? (tx - 8): (8 - tx));
       rx = tx + SIGMA_32AM_of_512QAM * gasdev();
n = (-1.0) / (2 * SIGMA_32AM_of_512QAM * SIGMA_32AM_of_512QAM);
       L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) + exp(n*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                    \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5))+
                                    exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
                                    \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                                    \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                                    \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
                                 (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                    \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                                    \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                                    \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
       L d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5))
                                    exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
                                 (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                                    \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                                   \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                                   \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
                                   \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
       L d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                                   exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
                                   \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                                   \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                                   exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
                                 (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                                   exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
```

```
\exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)));
L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                    \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                    exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
                    \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                    \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                    \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                    \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                    \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
                  (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                    \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                    \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                    \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                    \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                    \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                    \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                    \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                    \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                    \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                    \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-13.5)*(rx-13.5)))
                  (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                   \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
                   \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-15.5)*(rx-15.5))));
 D1_data[i]
                          = L_d0;
 D1 data[i+1]
                         = L d1;
D1 data[i+2]
                         = L d2;
D1_data[i+3]
                         = L_d3;
                         = L_d4;
D1 parity[i]
D1_parity[i+1] = 0.0;
D1_parity[i+2] = 0.0;
D1_parity[i+3] = 0.0;
D1_parity[i+5] = 0.0;
 /* symbol 1, I dimension: 16AM */
 d0 = data_d[i+4];
 d1 = data d(i+5);
 d2 = Encl[i+4];
d3 = Enc2[i+2];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_16AM_of_512QAM * gasdev();
n = (-1.0) / (2 * SIGMA 16AM of 512QAM * SIGMA 16AM of 512QAM);
L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5)) + 
                   exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                  (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
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\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)));
L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
           (exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
            \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
            \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
           (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
            \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5))));
D1_data[i+4]
                = L_d0;
                = L d1;
D1 data[i+5]
D1_parity[i+4] = L_d2;
D2 parity[i+2] = L d3;
D2 parity[i]
              = 0.0;
D2_parity[i+1] = 0.0;
D2 parity[i+3] = 0.0;
D2 parity[i+4] = 0.0;
D2 parity[i+5] = 0.0;
/* symbol 2, Q dimension: 32AM */
d0 = data_d[i+6];
d1
   = data_d[i+7];
d2
   = data_d(i+8);
d3 = data d[i+9];
d4
   = Enc2[i+6];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4): (4 - tx));
tx = (d0 == 0 ? (tx - 8): (8 - tx));
rx = tx + SIGMA_32AM_of_512QAM * gasdev();
   = (-1.0) / (2 * SIGMA 32AM of 512QAM * SIGMA 32AM of 512QAM);
L d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) + exp(n*(rx-1.5))*(rx-1.5))
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)));
L_dl = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
           (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
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\exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                   \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                    exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
                   \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                   \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)))
                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5))+
                   \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5))));
L d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))) + exp(n*(rx+1.5)) +
                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                   \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                   \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                   \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
                  (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                   \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                   \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                   \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                   \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                   \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-13.5)*(rx-13.5)))
                  (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                   \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
                   \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                   exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                   \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
                   \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                   exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5))));
 D1 data[i+6]
                          = L_d0;
D1_data[i+7]
                          = L d1;
D1_data[i+8]
                         = L_d2;
D1 data[i+9]
                         = L d3;
D2_parity[i+6] = L_d4;
D2_{parity[i+7]} = 0.0;
D2 parity[i+8] = 0.0;
D2 parity[i+9] = 0.0;
D2 parity[i+11] = 0.0;
 /* symbol 2, I dimension: 16AM */
d0 = data_d[i+10];
dl = data d[i+11];
d2 = Enc2[i+10];
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d3 = Encl[i+8];
              tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
              tx = (d0 == 0 ? (tx - 4): (4 - tx));
              rx = tx + SIGMA_16AM_of_512QAM * gasdev();

n = (-1.0) / (2 * SIGMA_16AM_of_512QAM * SIGMA_16AM_of_512QAM);
              L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                                  (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
                                   \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
              L dl = log((exp(n*(rx+3.5)*(rx+3.5))) + exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)))
                                  (\exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
                                   \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
                                   \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5))));
              L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) + exp(n*(rx+6.5)) + 
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)))
                                  (\exp(n*(rx+5.5)*(rx+5.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                                   \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5))));
             L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) + exp(n*(rx+6.5)))
                                   \exp(n*(rx+1.5)*(rx+1.5))+\exp(n*(rx+2.5)*(rx+2.5)) +
                                   \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
                                   \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)))
                                  (\exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+4.5)*(rx+4.5)) +
                                   \exp(n*(rx+3.5)*(rx+3.5))+\exp(n*(rx+0.5)*(rx+0.5)) +
                                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
                                   \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-7.5)*(rx-7.5)));
              D1 data[i+10]
                                            = L d0;
                                           = L_d1;
              D1_data[i+11]
              D2_parity[i+10] = L_d2;
             D1_parity[i+8] = L_d3;
             D1_parity[i+6]
                                          = 0.0;
             Dl_parity[i+7]
                                          = 0.0;
             D1_parity[i+9]
                                          = 0.0;
              D1_parity[i+10] = 0.0;
             D1_parity[i+11] = 0.0;
              i = i+11:
            interleave data:
       r ileav(D1 data, rule);
#endif
#ifdef R710 1024QAM
         * Use S2044_33_1 interleaver (multiple of 14)
         * I and Q dimensions:
         * d0 is MSB and d4 is LSB in 32AM: (d0,d1,d2,d3,d4):
                       \tt 00010--00011--00001--00000--00100--00101--00111--00110
                        -15.5 -14.5 -13.5 -12.5 -11.5 -10.5 -9.5
                       01010--01011--01001--01000--01100--01101--01111--01110
```

```
-0.5
               -1.5
                       -2.5
                               -3.5
                                       -4.5
                                              -5.5
                                                     -6.5
                                                             -7.5
         11010--11011--11001--11000--11100--11101--11111--11110
                        2.5
                               3.5
                                       4.5
                                              5.5
         10010--10011--10001--10000--10100--10101--10111--10110
         15.5 14.5 13.5 12.5 11.5 10.5 9.5
 */
    = (-1.0) / (2 * SIGMA 710 1024QAM * SIGMA 710 1024QAM);
for (i = 0; i < INT SIZE; i++)
    /* symbol 1, Q dimension */
    d0
       = data[i];
       = data[i+1];
    d1
   d2 = data[i+2];
      = data[i+3];
   d3
   d4 = Enc1[i];
   tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
   tx = (d1 == 0 ? (tx - 4): (4 - tx));

tx = (d0 == 0 ? (tx - 8): (8 - tx));
   rx = tx + SIGMA 710 1024QAM * qasdev();
   L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5)) + \exp(n*(rx-5.5)*(rx-5.5)) +
               \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
               \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
               \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
              (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
               \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
               \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
               \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
               \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
               \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)));
   L d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
               \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
                \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
               (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
               \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
                \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
               \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
                \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
                \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
   L d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
               \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
                \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
                \exp(n^*(rx+10.5)^*(rx+10.5)) + \exp(n^*(rx+11.5)^*(rx+11.5)) +
               \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
                \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
               \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
                \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)))
               (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
               \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
               \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
               \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
               \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
               \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5))
```



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\exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)));
L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5))+
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-13.5)*(rx-13.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-15.5)*(rx-15.5))));
D1_data[i]
                = L d0;
Dl data[i+1]
                = L d1;
D1_data[i+2]
               = L_d2;
               = L_d3;
D1 data[i+3]
               = L d4;
D1_parity[i]
D1_parity[i+1] = 0.0;
D1 parity[i+2] = 0.0;
Dl_parity[i+3] = 0.0;
D1 parity[i+4] = 0.0;
D1 parity[i+6] = 0.0;
/* symbol 1, I dimension */
d0 = data[i+4];
d1 = data[i+5];
d2 = data[i+6];
d3 = Enc1[i+5];
d4 = Enc2[i];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4): (4 - tx));
tx = (d0 == 0 ? (tx - 8): (8 - tx));
rx = tx + SIGMA 710 1024QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
           \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
           \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
           exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
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\exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
           \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
           (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
           \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
           \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
           \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
           \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
           \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
           \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
           \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
           \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
           \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
           \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5))));
L d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
           \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
           \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-14.5)*(rx-14.5)) + \exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
           \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
           \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
           exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
           \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
           \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
           \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
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\exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-15.5)*(rx-15.5))));
D1 data[i+4]
               = L d0;
D1 data[i+5]
               = L d1;
D1 data[i+6]
               = L_d2;
D1 parity[i+5] = L d3;
              = L_d4;
D2_parity[i]
D2 parity[i+1] = 0.0;
D2_{parity[i+2]} = 0.0;
D2_parity[i+3] = 0.0;
D2_parity[i+4] = 0.0;
D2 parity[i+6] = 0.0;
/* symbol 2, Q dimension */
   = data[i+7];
d1 = data[i+8];
d2 = data[i+9];
d3 = data[i+10];
d4 = Enc2[i+5];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1)) < 0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4): (4 - tx));
tx = (d0 == 0 ? (tx - 8): (8 - tx));
rx = tx + SIGMA_710 1024QAM * gasdev();
L d0 = \log((\exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L dl = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
           (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5))
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)));
L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
```

```
\exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
           \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)));
L d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
           \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
           \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
           \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
           \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
           \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
           \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5))) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
           exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
           \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
           \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
           \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
           \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-13.5)*(rx-13.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
           \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
            exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
           \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
           \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
           \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
           \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-15.5)*(rx-15.5))));
D1 data[i+7]
                = L d0;
D1 data[i+8]
               = L_d1;
D1_data(i+9)
               = L_d2;
D1_data[i+10] = L_d3;
D2 parity[i+5] = L d4;
D2 parity[i+7] = 0.0;
D2_parity[i+8] = 0.0;
D2 parity[i+9] = 0.0;
D2_{parity[i+11]} = 0.0;
D2_parity[i+12] = 0.0;
D2 parity[i+13] = 0.0;
/* symbol 2, I dimension */
d0 = data[i+11];
d1 = data[i+12];
d2 = data[i+13];
d3 = Enc2[i+10];
d4 = Encl[i+10];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4): (4 - tx));
tx = (d0 == 0 ? (tx - 8): (8 - tx));
rx = tx + SIGMA_710_1024QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
           \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
           \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
           \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
           \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
           \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5))
           \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
           \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
           \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
           \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
```

```
\exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5))
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L dl = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-4.5)*(rx-4.5)) + \exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)))
           (\exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5))));
L d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5))
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-11.5)*(rx-11.5)))
           (\exp(n*(rx+0.5)*(rx+0.5))+\exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5))
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5))));
L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+7.5)*(rx+7.5)) +
            \exp(n*(rx+8.5)*(rx+8.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-0.5)*(rx-0.5)) + \exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-7.5)*(rx-7.5)) +
            \exp(n*(rx-8.5)*(rx-8.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-15.5)*(rx-15.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+2.5)*(rx+2.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-13.5)*(rx-13.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-10.5)*(rx-10.5)));
L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            \exp(n*(rx+6.5)*(rx+6.5))+\exp(n*(rx+5.5)*(rx+5.5)) +
            \exp(n*(rx+10.5)*(rx+10.5))+\exp(n*(rx+9.5)*(rx+9.5)) +
            \exp(n*(rx+14.5)*(rx+14.5))+\exp(n*(rx+13.5)*(rx+13.5)) +
            \exp(n*(rx-2.5)*(rx-2.5))+\exp(n*(rx-1.5)*(rx-1.5)) +
            \exp(n*(rx-6.5)*(rx-6.5))+\exp(n*(rx-5.5)*(rx-5.5)) +
            \exp(n*(rx-10.5)*(rx-10.5))+\exp(n*(rx-9.5)*(rx-9.5)) +
            \exp(n*(rx-14.5)*(rx-14.5))+\exp(n*(rx-13.5)*(rx-13.5)))
           (\exp(n*(rx+4.5)*(rx+4.5))+\exp(n*(rx+3.5)*(rx+3.5)) +
            \exp(n*(rx+7.5)*(rx+7.5))+\exp(n*(rx+8.5)*(rx+8.5)) +
            \exp(n*(rx+12.5)*(rx+12.5))+\exp(n*(rx+11.5)*(rx+11.5)) +
            exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
            \exp(n*(rx-4.5)*(rx-4.5))+\exp(n*(rx-3.5)*(rx-3.5)) +
            \exp(n*(rx-7.5)*(rx-7.5))+\exp(n*(rx-8.5)*(rx-8.5)) +
```

```
\exp(n*(rx-12.5)*(rx-12.5))+\exp(n*(rx-11.5)*(rx-11.5)) +
                   \exp(n*(rx-0.5)*(rx-0.5))+\exp(n*(rx-15.5)*(rx-15.5))));
        D1_data[i+11]
                        = L_d0;
        D1_data[i+12]
                        = L_d1;
        D1 data[i+13]
                        = L d2;
       D2_parity[i+10] = L_d3;
       D1 parity[i+10] = L d4;
       D1_parity[i+7] = 0.0;
       D1_parity[i+8]
                       = 0.0;
       D1_parity[i+9] = 0.0;
       D1_parity[i+11] = 0.0;
       D1_parity[i+12] = 0.0;
       D1_parity[i+13] = 0.0;
       i = i+13;
#endif
    * At this moment we received the whole turbo code block:
    * D1_data[] stores the received information sequence,
    * D1_parity[] stores the received punctured parity P sequence and
    * D2_data[] stores the interleaved received information sequence,
   */
    for(i = 0; i < INT_SIZE; i++)
      D2 data[i] = D1 data[i];
    r_ileav(D2_data, rule);
    * D2_parity[] stores the received punctured parity Q sequence.
    for(iteration = 1; iteration <= NR ITER; iteration++)</pre>
        * Start one iteration of the turbo decoder here:
#ifdef R46_64QAM TTCM VoCAL
       jat map2(jat code1, D1 data, D1 parity, D1 app, D1 exi);
#else
       jat_map1(jat_code1, D1_data, D1_parity, D1_app, D1_exi);
#endif
        * Interleave the extrinsic information from Decoder1:
       for(k = 0; k < INT_SIZE; k++)
         D2_app[k] = D1_exi[k];
       r_ileav(D2_app, rule);
        * Decoder2:
#ifdef R46_64QAM_TTCM_VoCAL
       jat_map2(jat_code2, D2_data, D2_parity, D2_app, D2_exi);
#else
       jat_map1(jat_code2, D2 data, D2 parity, D2 app, D2 exi);
#endif
        * Deinterleave the extrinsic information from Decoder2:
       r_deileav(D2_exi, rule);
       for(k = 0; k < INT_SIZE; k++)
         D1_app[k] = D2_exi[k];
```

```
#ifdef R46_64QAM_TTCM_VoCAL
        for(k = 0; k < INT SIZE/2; k++)
          Dec data[k] = D1 data[k] + log(D1_exi[k]) + log(D2_exi[k]);
         * Re-encode with encoder1:
        jat_code1->enc_state = 0;
                                               /* reset encoder1's state
        for (k = 0; k < INT_SIZE/2; k++)
          Encl[k] = jat_enc_bp_fp(jat_code1, ((Dec_data[k] > 0.0)?1:0));
         * interleave data:
         */
          for(k = 0; k < INT_SIZE/2; k++)
           data i[k] = ((Dec data[k] > 0.0)?1:0);
         r ileava(data i, rule);
          * • Re-encode with encoder2:
          */
        jat_code2->enc_state = 0;
                                               /* reset encoder2's state
         for (k = 0; k < INT SIZE/2; k++)
            Enc2[k] = jat_enc_bp_fp(jat_code2, data_i[k]);
          \mbox{^{\star}} Find the closest point out of four in the sub-constellation
          */
        for (k = 0; k < INT_SIZE/2 - 1;)
            u4 = ((Dec_data[k] > 0.0)?1:0);

u3 = ((Dec_data[k+1] > 0.0)?1:0);
             u2 = Encl[k];
            u1 = Enc2[k+1];
             rx I = D1 data[k + INT SIZE/2];
             rx_Q = D1_data[k + INT_SIZE/2 + 1];
             j = 4*u4+8*u3+16*u2+32*u1;
             v00_I = find_tx_I(j);
             v00_Q = find_tx_Q(j);
             v01_I = find_tx_I(j+1);
             v01_Q = find_tx_Q(j+1);
            v10_I = find_tx_I(j+2);
v10_Q = find_tx_Q(j+2);
             v11_I = find_tx_I(j+3);
             v11_Q = find_tx_Q(j+3);
             Dec_data[k+INT_SIZE/2] = log(
                      (\exp(n^*((rx_I-v11_I)*(rx_I-v11_I)+(rx_Q-v11_Q)*(rx_Q-v11_Q)))+
                     exp(n*((rx_I-v10_I)*(rx_I-v10_I)+(rx_Q-v10_Q)*(rx_Q-v10_Q))))/
(exp(n*((rx_I-v01_I)*(rx_I-v01_I)+(rx_Q-v01_Q)*(rx_Q-v01_Q)))+
                      exp(n*((rx_I-v00_I)*(rx_I-v00_I)+(rx_Q-v00_Q)*(rx_Q-v00_Q)))));
             Dec_data[k+INT_SIZE/2+1] = log(
                     (\exp(n^*((rx_I-v11_I)*(rx_I-v11_I)+(rx_Q-v11_Q)*(rx_Q-v11_Q)))+
                      exp(n*((rx_I-v01_I)*(rx_I-v01_I)+(rx_Q-v01_Q)*(rx_Q-v01_Q))))/
                     (exp(n*((rx_I-v10_I)*(rx_I-v10_I)+(rx_Q-v10_Q)*(rx_Q-v10_Q)))+
exp(n*((rx_I-v00_I)*(rx_I-v00_I)+(rx_Q-v00_Q)*(rx_Q-v00_Q)))));
            k = k+2;
#else
        for(k = 0; k < INT_SIZE; k++)
          Dec_data[k] = D1_data[k] + log(D1_exi[k]) + log(D2_exi[k]);
#endif
```

```
* print errors:
        k = print_err(data, Dec_data, iteration, block, no_err);
        if(k == 0)
          break;
         * End one iteration of the turbo decoder here.
  }
free(jat_code1->P0state);
free(jat_code1->Plstate);
free(jat_code1->N0state);
free(jat code1->N1state);
free(jat_code1->Coded0);
free(jat_code1->Coded1);
free(jat code1);
free(jat_code2->P0state);
free(jat_code2->P1state);
free(jat_code2->N0state);
free(jat code2->N1state);
free(jat_code2->Coded0);
free(jat_code2->Coded1);
free(jat code2);
free(rule);
free(data);
free(data_i);
free(data d);
free(no err);
free(Enc1);
free (Enc2);
free(D1 data);
free(D1_parity);
free(D1_app);
free(D1_exi);
free(D2_data);
free(D2_parity);
free(D2_app);
free(D2_exi);
free (Dec_data);
free(frame hist);
free(Zero_data);
for(i = THRESHOLD ITER; i <= NR ITER; i++)</pre>
        free(bit_hist_array[i]);
free(bit_hist_array);
free(bit_hist_block);
^{\prime\prime} jat_trellis_bp_fp() initializes the code structure
void jat_trellis_bp_fp(jat_code *code_str)
  int i;
  for(i = 0; i < code_str->nr_states ; i++)
      code_str->enc state = i;
       code_str->POstate[i] = jat_ps(code_str, 0);
      code_str->Plstate[i] = jat_ps(code_str, 1);
      code_str->enc_state = i;
       code str->Coded0[i] = jat_enc_bp_fp(code_str, 0);
      code_str->NOstate[i] = code_str->enc_state;
                                                       /*next state i if d = 0 */
      code_str->enc_state = i;
      code_str->Coded1[i] = jat_enc_bp_fp(code_str, 1);
       }
```



```
/* jat ps() returns the previous state, given the code structure & the input ^{*}/
       bit for the previous state
            /*
int jat_ps(jat_code *code_st, int inp)
 int pr_state, pr_msb, i, j, k, l;
 if(code_st->enc_mem == 1)
     pr_state = code_st->enc_state ^ inp;
 else
    {
     /*find previous state:
     pr_msb = (inp & 0x1) ^ (code_st->enc_state & 0x1);
     for (i=1, j=2, k=(1
                             <<
                                      code st->enc mem-1), l=code st->enc mem-1; i<code st-
>enc_mem; i++, l--)
       {
         pr msb = pr msb ^ (((code st->enc state&j)>>i) & ((code st->bp&k)>>l));
         j = j << 1;
         k = k >> 1;
       }
     pr_state = ((code_st->enc_state >> 1) & ((1<<(code_st->enc_mem - 1)) - 1)) |
       (pr msb << (code st->enc mem - 1));
 return (pr_state);
  jat_enc_bp_fp() - rate 1/2 systematic feedback convolutional enc.
           input: input bit to be encoded
/*
           output: the coded bit
/* Note:
           the lsb of the enc_state will have the new input bit
           the msb of the enc state matches the lsb of bp & fp
int jat_enc_bp_fp(jat_code *code_st, int data)
 int new_lsb, parity, i, j, k, l;
 new lsb = data;
 if(code_st->enc_mem == 1)
   {
     parity = code_st->enc_state ^ data;
     code_st->enc_state = parity;
   }
 else
     /* xor it with the bits of the enc_state1 for which bpl is one
     for(i = 0, j = 1, k = (1 << code st->enc mem-1), l = code st->enc mem - 1; <math>i <
code_st->enc_mem; i++, 1--)
      {
        new_lsb = new_lsb ^ (((code_st->enc_state&j)>>i) & ((code_st->bp&k)>>l));
         j = j << 1;
         k = k \gg 1;
       }
     /* find the parity bit
     parity = new_lsb & ((code_st->fp&(1<<code_st->enc_mem)) >> code_st->enc_mem);
     for(i = 0, j = 1, k = (1 << code_st->enc_mem-1), l = code_st->enc_mem - 1; i <
code st->enc mem; i++, 1--)
      {
         parity = parity ^ (((code_st->enc_state&j)>>i) & ((code st->fp&k)>>l));
         j = j << 1;
         k = k >> 1;
```



```
new_lsb;
 return (parity);
void r_ileav(double *array, int *rule_i)
 double *i_wmem;
     k;
 int
 i wmem = (double *)malloc(sizeof(double) * INT SIZE);
 if(i wmem == 0)
   printf("\nCouldn't allocate i_wmem memory!");
 for (k = 0; k < INT SIZE; k++)
   i_wmem[k] = array[k];
 for(k = 0; k < INT SIZE; k++)
   array[k] = i_wmem[rule_i[2*k+1]];
 free(i_wmem);
}
void r_ileava(int *array, int *rule_i)
 int *i_wmem;
 int k;
 i_wmem = (int *)malloc(sizeof(int) * INT SIZE);
 if(i wmem == 0)
   printf("\nCouldn't allocate i_wmem memory!");
 for(k = 0; k < INT_SIZE; k++)
   i_wmem[k] = array[k];
 for(k = 0; k < INT SIZE; k++)
   array[k] = i_wmem[rule_i[2*k+1]];
  free(i_wmem);
void r_deileav(double *array, int *rule_d)
 double *d_wmem;
 int
 d_wmem = (double *)malloc(sizeof(double) * INT SIZE);
 if(d_wmem == 0)
   printf("\nCouldn't allocate d wmem memory!");
 for(k = 0; k < INT_SIZE; k++)
   d_wmem[rule_d[2*k+1]] = array[k];
 for(k = 0; k < INT SIZE; k++)
   array[k] = d_wmem[k];
 free(d wmem);
}
/******************************
void r_deileava(int *array, int *rule_d)
 int
       *d wmem;
 int
       k:
 d_wmem = (int *)malloc(sizeof(int) * INT_SIZE);
 if(d wmem == 0)
   printf("\nCouldn't allocate d_wmem memory!");
 for(k = 0; k < INT_SIZE; k++)
   d_{wmem[rule_d[2*k+1]]} = array[k];
 for (k = 0; k < INT_SIZE; k++)
```

```
array[k] = d wmem[k];
  free(d_wmem);
/*********************
/* nrgen() returns a random number between 0 and 1
     (uniform distribution generator)
double nrgen()
  long z, k;
  k = s1 / 53668;
  s1 = 40014 * (s1 - k * 53668) - k * 12211;
  if(s1 < 0)
  s1 += 2147483563;
  k = s2 / 52774;
  s2 = 40692 * (s2 - k * 52774) - k * 3791;
  if(s2 < 0)
  s2 += 2147483399;
z = s1 - s2;
  if(z < 1)
  z += 2147483562;
  return ((double)z / 2147483563);
/* nrgenbin() returns a 0 or 1 (uniform distribution)
int nrgenbin()
 return ((nrgen() > 0.5)?1:0);
/* gasdev() returns a normally distributed deviate
    with zero mean and unit variance
double gasdev()
  static int
               iset = 0;
  static double gset;
                fac, r, v1, v2;
  double
  if(iset == 0)
      /* pick two uniform numbers in the square extending from
      /\star -1 to +1 in each direction, see if they are in the
      /* unit circle, and if they are not, try again.
      do
         v1 = 2.0 * nrgen() - 1.0;
v2 = 2.0 * nrgen() - 1.0;
         r = v1 * v1 + v2 * v2;
      while (r >= 1.0 || r == 0.0);
      fac = sqrt(-2.0 * log(r)/r);
      /* now make the Box-Muller transformation to get two normal
      /* deviates; return one and save the other for next time.
      gset = v1 * fac;
                          /* set flag
      iset = 1;
      return (v2 * fac);
    }
  else
      /\star we have an extra deviate handy, so unset the flag and
      /* return it.
     iset = 0;
      return (gset);
}
```

```
/* errors() returns the nr. of positions in which two blocks of data are
            different; it accepts a shift between the addresses
/*
            inputs: the address of the first block of integers
/*
                    the address of the second block of doubles
/*
                    the size of the block (blocks are equal)
            output: the number of positions in which the two blocks are dif.
int errors(int *block1, double *block2, int size, int iter nr)
 int count = 0;
  for(i = 0; i < size; i++)
      if(block1[i] != ((block2[i] > 0.0)?1:0))
       {
         count++;
#if defined BIT HIST
         if(iter_nr>=THRESHOLD_ITER)
             *bit_hist_array[iter_nr] = bit_hist_block[iter_nr];
             bit_hist_array[iter_nr]++;
             *bit_hist_array[iter_nr] = i;
             bit_hist_array[iter_nr]++;
#endif
#if defined BIT_HIST
  if((count>0)&&(iter_nr >= THRESHOLD_ITER))
   bit hist block[iter nr]++;
#endif
 return (count);
/* print_err() append to the file the nr. of errors and BER
/* returns: number of bit errors in a block
int print_err(int *data1, double *data2, int iter_no, int block_no, int *err)
{
 int
       i, j, nr;
      block_err = 0;
 char fname[] = BIT_HIST_FILE_NAME;
char sss[] = {'0','1','2','3','4','5','6','7','8','9'};
 FILE *out_file = NULL;
 int *pi;
 if((iter_no == 1) && (block_no == 1))
      out file = fopen(ERROR FILE NAME, "a");
      if(!out_file)
       {
         printf("Error2: the output file could not be opened!\n");
         exit (1);
      fprintf(out_file, "ref_tc.c, RSC1_enc_mem = %d, RSC1 fp = %d, RSC1 bp = %d,
RSC2_enc_mem = %d, RSC2_fp = %d, RSC2_bp = %d, s1 = %d, s2 = %d, int_size = %d, Limit soft
outputs to = %e, Eb/No = %fdB\n", RSC1 ENC MEM, RSC1 FP, RSC1 BP, RSC2 ENC MEM, RSC2 FP,
RSC2_BP, SEED1, SEED2, INT_SIZE, (double) MAX, (double) EBNO);
     fclose(out file);
 block_err = errors(data1, data2, INT_SIZE, iter_no);
 err[iter no - 1] += block err;
 ++frame hist[(iter no-1)*(INT SIZE+1) + block err];
 if((iter_no == NR_ITER) && (block_err != 0))
   ++frame err;
```

```
#if defined BIT HIST
 if((block_err != 0) && (iter_no >= THRESHOLD_ITER))
      fname[strlen(fname)-1]= sss[iter no];
      out_file = fopen(fname, "a");
      if(!out_file)
       {
         printf("Error: the bit hist file could not be opened!\n");
      for(pi = bit_hist_array[NR_ITER +iter_no]; pi < bit_hist_array[iter_no]; pi = pi+2)</pre>
       fprintf(out_file, "\n%06d %06d", *pi, *(pi+1));
      fclose(out_file);
      bit_hist_array[iter_no] = bit_hist_array[NR_ITER +iter_no];
#endif
 if(((iter_no == NR_ITER) && (((block_no % PRINT_BLOCKS) == 0) || (err[NR_ITER - 1] >
MAX ERRORS))) || (((block_no % PRINT_BLOCKS) == 0) && (block err == 0)))
       out_file = fopen(ERROR_FILE_NAME, "a");
       if(!out file)
           printf("Error3: the output file could not be opened!\n");
            exit (1);
       nr = block no * INT SIZE;
       fprintf(out_file, "\n\n\n. of info bits: %d (%d blocks)",
       nr, block_no);
for(j = 0; j < NR_ITER; j++)</pre>
         fprintf(out_file, "\nIter: %02d, Errors: %06d, BER = %e",
                 j + 1, err[j], (double)err[j]/INT_SIZE/block_no);
       total_err = err[NR_ITER - 1];
       fprintf(out file, "\nFrame error = %f(%f errors per block)\n",
               (double) frame_err/block_no,
               (frame_err == 0?0.0:(double)err[NR_ITER-1]/frame_err));
       fclose(out_file);
       if((block no % 100000) == 0)
            out_file = fopen(FRAME_HIST_FILE_NAME, "a");
            if(!out_file)
               printf("Error4: the .fhist file could not be opened!\n");
               exit (1);
            nr = block no * INT SIZE;
            fprintf(out file, "\n\nNr. of info bits: %d (%d blocks)",
            nr, block_no);
for(j = 0; j <= INT_SIZE; j++)
  fprintf(out_file, "\n%03d %03d",</pre>
                      j, frame_hist((NR_ITER-1)*(INT_SIZE+1)+j));
            fclose(out_file);
return (block_err);
/* This is a MAP decoder for a cs->nr_states states jat_code.
     function: decodes a block of received data of length INT SIZE.
                It assumes that the encoder state starts from state zero
                code structure, I address, Q address, L in address
    output:
                the extrinsic information in L\_{out}
     globals:
                noise
```

```
* As jat_map but outputs probability and not log(probability)
  * It also can handle very large interleavers
 void jat map1(jat code *cs, double *I, double *Q, double *L in, double *L out)
  {
    double
              sum, sum_0, sum_1, max;
             i, j, k, st;
   int
   double
             *alpha_old;
   double
              *alpha_new;
              *beta0;
   double
   double
             *beta1;
             *probI;
   double
   double
              *probQ;
 alpha_old = (double *)malloc(sizeof(double) * 2 * cs->nr states);
 alpha_new = (double *)malloc(sizeof(double) * 2 * cs->nr states);
 beta0 = (double *)malloc(sizeof(double) * INT SIZE * cs->nr states);
 if(beta0 == 0)
     printf("Couldn't allocate beta0 memory!\n");
      exit(1);
   }
betal = (double *)malloc(sizeof(double) * INT_SIZE * cs->nr states);
 if(beta1 == 0)
     printf("Couldn't allocate beta1 memory!\n");
     exit(1);
   }
 probI = (double *)malloc(sizeof(double) * INT SIZE);
 if(probI == 0)
     printf("Couldn't allocate probI memory!\n");
     exit(1);
   }
 probQ = (double *)malloc(sizeof(double) * INT_SIZE);
 if(probQ == 0)
     printf("Couldn't allocate probQ memory!\n");
     exit(1);
   }
    /* initialize the alpha_old metrics
                                                                                */
   for(st = 0; st < cs->nr_states; st++)
     for (k = 0; k < 2; k++)
       *(alpha_old + k * cs->nr_states + st) = 0.0;
   *(alpha_old + cs->Postate[0]) = 1.0;
   *(alpha_old + cs->nr_states + cs->P1state[0]) = 1.0;
    /* initialize beta's
                                                                                */
   for(st = 0; st < cs->nr states; st++)
       beta0[(INT_SIZE - 1) * cs->nr_states + st] = 1.0;
       betal[(INT_SIZE - 1) * cs->nr_states + st] = 1.0;
   /* compute all beta's
                                                                                */
   for (i = INT SIZE - 2; i >= 0; i--)
         probI[i + 1] = exp(I[i + 1]) * L_in[i + 1];
         probQ[i + 1] = exp(Q[i + 1]);
         for(st = 0; st < cs->nr_states; st++)
             /* compute beta0[i][st]:
                                                                                */
```

```
beta0[i * cs->nr states + st] = beta0[(i + 1) * cs->nr states + cs-
>NOstate[st]]*
                           ((cs->Coded0[cs->N0state[st]] == 0)?1:probQ[i + 1])+
                           betal[(i + 1) * cs->nr states + cs->NOstate[st]]*probI[i + 1]*
                           ((cs->Coded1[cs->N0state[st]] == 0)?1:probQ[i + 1]);
                          cs->nr states + st] = beta0[(i + 1) * cs->nr states + cs-
>N1state[st]]*
                           ((cs->Coded0[cs->N1state[st]] == 0)?1:probQ[i + 1])+
                           beta1[(i + 1) * cs->nr states + cs->N1state[st]]*probI[i + 1]*
                           ((cs->Coded1[cs->N1state[st]] == 0)?1:probQ[i + 1]);
         } -
       max = beta0[i * cs->nr_states];
       for(st = 1; st < cs->nr_states; st++)
         if(beta0[i * cs->nr_states + st] > max)
           max = beta0[i * cs->nr states + st];
       for(st = 0; st < cs->nr_states; st++)
         if(betal[i * cs->nr states + st] > max)
           max = betal[i * cs->nr_states + st];
       for(st = 0; st < cs->nr states; st++)
           beta0[i * cs->nr_states + st] = beta0[i * cs->nr_states + st] / max;
           beta1[i * cs->nr states + st] = beta1[i * cs->nr states + st] / max;
      }
  /* now we have all beta's; we can compute alpha for all states for each
 /* data bit and using beta's we compute lambda
probI[0] = exp(I[0]) * L in[0];
  probQ[0] = exp(Q[0]);
  for (k = 0; k < INT_SIZE; k++)
      for(st = 0; st < cs->nr_states; st++)
       sum = *(alpha_old + cs->POstate[st]) + *(alpha_old + cs->nr_states + cs-
>P1state[st]);
       *(alpha new + st) = sum * ((cs->Coded0[st] == 0)?1:probQ[k]);
       *(alpha_new + cs->nr_states + st) = sum * probI[k] * ((cs->Coded1[st] ==
0)?1:probQ[k]);
       }
      /* find the max value and renormalize alpha's:
      max = *alpha_new;
      for(st = 0; st < cs->nr_states; st++)
       for(j = 0; j < 2; j++)
         if(*(alpha_new + cs->nr_states * j + st) > max)
                max = *(alpha_new + cs->nr_states * j + st);
      for(st = 0; st < cs->nr_states; st++)
       for(j = 0; j < 2; j++)
          *(alpha_new + cs->nr_states * j + st) = *(alpha_new + cs->nr_states * j + st)/
max;
      /* find sum 0 and sum 1 over all states for L out:
      sum 0 = 0.0;
      sum 1 = 0.0;
      for(st = 0; st < cs->nr states; st++)
         sum_0 += *(alpha_new + st) * beta0[k * cs->nr_states + st];
         sum 1 += *(alpha_new + cs->nr_states + st) * betal{k * cs->nr_states + st};
      /* output the extrinsic information:
                                                                              */
      L_{out[k]} = (sum_1 / sum_0) / exp(I[k]) / L_in[k];
      if(L_out[k] > MAX)
       L out[k] = MAX;
      if(L_out[k] < 1/MAX)
       L_{out}[k] = 1/MAX;
      for(st = 0; st < cs->nr_states; st++)
       for(j = 0; j < 2; j++)/* update alphas
         *(alpha_old + cs->nr_states * j + st)=*(alpha_new + cs->nr_states * j + st);
```



```
}
free(beta0);
free (beta1);
free (probI);
free(probQ);
free(alpha_old);
free(alpha_new);
double find_tx_I(int k)
  double tx I;
        switch(k)
        . {
         case 0:
           tx_I = 0.5;
           break;
         case 1:
           tx I = -3.5;
           break;
          case 2:
           tx_I = 0.5;
           break;
          case 3:
           tx_I = -3.5;
           break;
         case 4:
           tx_I = 2.5;
           break;
          case 5:
           tx_I = -1.5;
           break;
          case 6:
           tx I = 2.5;
           break;
          case 7:
           tx I = -1.5;
           break;
          case 8:
           tx I = 2.5;
           break;
         case 9:
           tx I = -1.5;
           break;
          case 10:
           tx_I = 2.5;
           break;
          case 11:
           tx_I = -1.5;
           break;
          case 12:
           tx_{x_{1}} = 0.5;
           break;
          case 13:
           tx_I = -3.5;
           break;
         case 14:
           tx_{x_i} = 0.5;
           break;
          case 15:
           tx_I = -3.5;
           break;
          case 16:
           tx_I = 1.5;
           break;
          case 17:
           tx I = -2.5;
           break;
```



```
case 18:
  tx_I = 1.5;
  break;
case 19:
 tx_I = -2.5;
  break;
case 20:
  tx_I = 3.5;
 break;
case 21:
 tx_I = -0.5;
  break;
case 22:
 tx_I = 3.5;
  break;
case 23:
  tx_I = -0.5;
 break;
case 24:
 tx I = 3.5;
 break;
case 25:
 tx I = -0.5;
 break;
case 26:
 tx I = 3.5;
 break;
case 27:
 tx I = -0.5;
 break;
case 28:
 tx_I = 1.5;
 break;
case 29:
 tx_I = -2.5;
 break;
case 30:
 tx_I = 1.5;
 break;
case 31:
 tx_I = -2.5;
 break;
case 32:
  tx_I = 1.5;
 break;
case 33:
 tx I = -2.5;
 break;
case 34:
 tx I = 1.5;
 break;
case 35:
 tx_I = -2.5;
 break;
case 36:
  tx I = 3.5;
 break;
case 37:
 tx_I = -0.5;
 break;
case 38:
 tx I = 3.5;
 break;
case 39:
  tx I = -0.5;
 break;
case 40:
 tx I = 3.5;
 break;
case 41:
 tx_I = -0.5;
```

}

```
break;
  case 42:
    tx_I = 3.5;
   break;
  case 43:
   tx_1 = -0.5;
   break;
  case 44:
   tx I = 1.5;
   break;
  case 45:
   tx_I = -2.5;
   break;
  case 46:
   tx_I = 1.5;
   break;
  case 47:
   tx_I = -2.5;
   break;
  case 48:
   tx I = 0.5;
   break;
  case 49:
   tx_I = -3.5;
   break;
  case 50:
   tx_I = 0.5;
   break;
  case 51:
   tx I = -3.5;
   break;
  case 52:
   tx I = 2.5;
   break;
  case 53:
   tx_I = -1.5;
   break;
  case 54:
   tx_I = 2.5;
   break;
  case 55:
   tx I = -1.5;
   break;
  case 56:
   tx I = 2.5;
   break;
  case 57:
   tx_I = -1.5;
   break;
  case 58:
   tx_I = 2.5;
   break;
  case 59:
   tx_I = -1.5;
   break;
  case 60:
   tx I = 0.5;
   break;
  case 61:
   tx_I = -3.5;
   break;
  case 62:
   tx_I = 0.5;
   break;
  case 63:
   tx_I = -3.5;
   break;
 }
return(tx_I);
```



```
double find_tx_Q(int k)
 double tx_Q;
       switch(k)
         case 0:
           tx_Q = 2.5;
           break;
         case 1:
           tx_Q = 2.5;
           break;
         case 2:
           tx Q = -1.5;
           break;
         case 3:
           tx_Q = -1.5;
           break;
         case 4:
           tx_Q = 0.5;
           break;
         case 5:
           tx Q = 0.5;
           break;
         case 6:
           tx Q = -3.5;
           break;
         case 7:
           tx_Q = -3.5;
           break;
         case 8:
          tx_Q = 2.5;
           break;
         case 9:
           tx_Q = 2.5;
           break;
         case 10:
           tx_Q = -1.5;
           break;
         case 11:
           tx_Q = -1.5;
           break;
         case 12:
           tx_Q = 0.5;
           break;
         case 13:
           tx_Q = 0.5;
           break;
         case 14:
           tx Q = -3.5;
           break;
         case 15:
          tx_Q = -3.5;
           break;
         case 16:
           tx_Q = 3.5;
           break;
         case 17:
         tx_Q = 3.5;
           break;
         case 18:
          tx_Q = -0.5;
           break;
         case 19:
           tx_Q = -0.5;
           break;
         case 20:
           tx Q = 1.5;
          break;
         case 21:
           tx_Q = 1.5;
```

```
break;
case 22:
  tx_Q = -2.5;
 break;
case 23:
 tx Q = -2.5;
 break;
case 24:
 tx Q = 3.5;
 break;
case 25:
 tx_Q = 3.5;
 break;
case 26:
 tx_Q = -0.5;
 break;
case 27:
 tx Q = -0.5;
 break;
case 28:
 tx_Q = 1.5;
 break;
case 29:
 tx_Q = 1.5;
 break;
case 30:
 tx_Q = -2.5;
 break;
case 31:
 tx_Q = -2.5;
 break;
case 32:
 tx_Q = 2.5;
 break;
case 33:
 tx_Q = 2.5;
 break;
case 34:
 tx_Q = -1.5;
 break;
case 35:
 tx_Q = -1.5;
 break;
case 36:
 tx_Q = 0.5;
 break;
case 37:
 tx_Q = 0.5;
 break;
case 38:
 tx Q = -3.5;
 break;
case 39:
 tx Q = -3.5;
 break;
case 40:
 tx_Q = 2.5;
 break;
case 41:
 tx_Q = 2.5;
 break;
case 42:
 tx_Q = -1.5;
 break;
case 43:
 tx_Q = -1.5;
 break;
case 44:
 tx_Q = 0.5;
 break;
```

case 45:

٢

}

COMPUTER PROGRAM LISTING APPENDIX

tx Q = 0.5;

```
break;
         case 46:
          tx Q = -3.5;
          break;
         case 47:
          tx_Q = -3.5;
          break;
         case 48:
          tx_Q = 3.5;
          break;
         case 49:
          tx Q = 3.5;
          break;
         case 50:
          tx_Q = -0.5;
          break;
         case 51:
          tx_Q = -0.5;
          break;
        case 52:
          tx_Q = 1.5;
          break;
         case 53:
          tx_Q = 1.5;
          break;
         case 54:
          tx_Q = -2.5;
          break;
        case 55:
          tx_Q = -2.5;
          break;
        case 56:
          tx Q = 3.5;
          break;
         case 57:
          tx Q = 3.5;
          break;
         case 58:
          tx Q = -0.5;
          break;
        case 59:
          tx Q = -0.5;
          break;
        case 60:
          tx Q = 1.5;
          break;
        case 61:
          tx_Q = 1.5;
          break;
        case 62:
          tx_Q = -2.5;
          break;
        case 63:
          tx Q = -2.5;
          break;
      return(tx Q);
/***********************
/* This is a MAP decoder for a cs->nr_states states jat_code.
/*
    function: decodes a block of received data of length INT_SIZE/2.
               It assumes that the encoder state starts from state zero
                                                                          */
               code structure, I address, Q address, L\_in address
    input:
    output:
               the extrinsic information in L_out
             noise
    globals:
```

```
* As jat_map but outputs probability and not log(probability)
 * It also can handle very large interleavers
void jat_map2(jat_code *cs, double *I, double *Q, double *L_in, double *L_out)
  double
            sum, sum_0, sum_1, max;
            i, j, k, st;
  int
  double
            *alpha_old;
  double
            *alpha_new;
  double
            *beta0;
  double
            *beta1;
  double
            *probI;
  double
            *probQ;
alpha_old = (double *)malloc(sizeof(double) * 2 * cs->nr_states);
alpha new = (double *)malloc(sizeof(double) * 2 * cs->nr states);
beta0 = (double *)malloc(sizeof(double) * INT_SIZE/2 * cs->nr_states);
if(beta0 == 0)
    printf("Couldn't allocate beta0 memory!\n");
    exit(1);
  }
beta1 = (double *)malloc(sizeof(double) * INT SIZE/2 * cs->nr states);
if(beta1 == 0)
    printf("Couldn't allocate beta1 memory!\n");
    exit(1);
  }
probI = (double *)malloc(sizeof(double) * INT_SIZE/2);
if(probI == 0)
 -{
    printf("Couldn't allocate probI memory!\n");
    exit(1);
  }
probQ = (double *)malloc(sizeof(double) * INT SIZE/2);
if(probQ == 0)
 {
    printf("Couldn't allocate probQ memory!\n");
    exit(1);
  /* initialize the alpha_old metrics
                                                                               */
  for(st = 0; st < cs->nr_states; st++)
   for (k = 0; k < 2; k++)
      *(alpha old + k * cs->nr states + st) = 0.0;
  *(alpha_old + cs->P0state[0]) = 1.0;
  *(alpha_old + cs->nr_states + cs->P1state[0]) = 1.0;
  /* initialize beta's
                                                                               * /
  for(st = 0; st < cs->nr states; st++)
      beta0[(INT\_SIZE/2 - 1) * cs->nr\_states + st] = 1.0;
      betal[(INT SIZE/2 - 1) * cs->nr states + st] = 1.0;
  /* compute all beta's
                                                                               */
  for (i = INT SIZE/2 - 2; i >= 0; i--)
      {
       probI[i + 1] = exp(I[i + 1]) * L in[i + 1];
       probQ[i + 1] = exp(Q[i + 1]);
       for(st = 0; st < cs->nr_states; st++)
           /* compute beta0[i][st]:
                                                                              */
```

```
beta0[i * cs->nr_states + st] = beta0[(i + 1) * cs->nr_states + cs-
>NOstate[st]]*
                          ((cs->Coded0[cs->N0state[st]] == 0)?1:probQ[i + 1])+
                          beta1[(i + 1) * cs->nr_states + cs->N0state[st]]*probI[i + 1]*
                          ((cs->Coded1[cs->N0state[st]] == 0)?1:probQ[i + 1]);
              betal[i *
                          cs->nr_states + st = beta0[(i + 1) * cs->nr_states + cs-
>N1state[st]]*
                          ((cs->Coded0[cs->N1state[st]] == 0)?1:probQ[i + 1])+
                          betal[(i + 1) * cs->nr\_states + cs->Nlstate[st]]*probI[i + 1]*
                          ((cs->Coded1[cs->N1state[st]] == 0)?1:probQ[i + 1]);
         }
       max = beta0[i * cs->nr states];
       for(st = 1; st < cs->nr_states; st++)
         if(beta0[i * cs->nr states + st] > max)
           max = beta0[i * cs->nr_states + st];
       for(st = 0; st < cs->nr states; st++)
         if(betal[i * cs->nr_states + st] > max)
           max = betal[i * cs->nr_states + st];
       for(st = 0; st < cs->nr_states; st++)
           beta0[i * cs->nr_states + st] = beta0[i * cs->nr_states + st] / max;
           betal[i * cs->nr_states + st] = betal[i * cs->nr_states + st] / max;
      }
/* now we have all beta's; we can compute alpha for all states for each
  /* data bit and using beta's we compute lambda
  probI[0] = exp(I[0]) * L_in[0];
  probQ[0] = exp(Q[0]);
  for (k = 0; k < INT_SIZE/2; k++)
      for(st = 0; st < cs->nr_states; st++)
       {
       sum = *(alpha_old + cs->P0state[st]) + *(alpha_old + cs->nr_states + cs-
>P1state[st]);
       *(alpha new + st) = sum * ((cs->Coded0[st] == 0)?1:probQ[k]);
       *(alpha_new + cs->nr_states + st) = sum * probI[k] * ((cs->Coded1[st] ==
0)?1:probQ[k]);
       }
      /* find the max value and renormalize alpha's:
     max = *alpha new;
      for(st = 0; st < cs->nr_states; st++)
       for(j = 0; j < 2; j++)
         if(*(alpha new + cs->nr states * j + st) > max)
                max = *(alpha_new + cs->nr_states * j + st);
      for(st = 0; st < cs->nr_states; st++)
       for(j = 0; j < 2; j++)
          *(alpha_new + cs->nr_states * j + st) = *(alpha_new + cs->nr_states * j + st)/
max;
      /* find sum_0 and sum_1 over all states for L out:
      sum_0 = 0.0;
      sum_1 = 0.0;
     for(st = 0; st < cs -> nr states; st++)
         sum 0 += *(alpha new + st) * beta0[k * cs->nr states + st];
         sum_1 += *(alpha_new + cs->nr_states + st) * betal[k * cs->nr_states + st];
      /* output the extrinsic information:
     L_{out[k]} = (sum 1 / sum 0) / exp(I[k]) / L in[k];
      if(L_out[k] > MAX)
       L out[k] = MAX;
      if(L out[k] < 1/MAX)
       L out[k] = 1/MAX;
      for(st = 0; st < cs->nr_states; st++)
       for(j = 0; j < 2; j++)/* update alphas
         *(alpha_old + cs->nr_states * j + st)=*(alpha_new + cs->nr states * j + st);
```



```
}
free(beta0);
free(beta1);
free(probI);
free(probQ);
free(alpha_old);
free(alpha_new);
}
```

interlever.c

```
#define MAX_CINDEX 46
#define MAX RINDEX 47
#define MAX ELEMENT 2100
#include <stdio.h>
#include <stdlib.h>
void main (void)
       int ra, ca; //Ia sequence row and column indices
       int count; //Counter for each bit in DMT frame
       int element; //Element number used for finding if element within array
       FILE *output;
       output=fopen("interleaver", "w");
       //Initial sequence indices
       ra=MAX_RINDEX-1;
       ca=0;
       //Adjust the initial indices for Ia if beyond ending element
       element=ra*MAX_CINDEX+ca;
       while (element >=MAX_ELEMENT) {
               ra--;
               ca++;
               if (ra<0) {
                       ra=MAX_RINDEX-1;
                       ca=ca+(MAX_RINDEX-1);
               ca=ca%MAX_CINDEX;
               element= ra*MAX_CINDEX+ra;
       //Fetch all elements in sequence Ia
       for (count = 0; count<MAX_ELEMENT; count++) {</pre>
               //Fetch array[ra][ca]
               element=ra*MAX_CINDEX+ca;
               fprintf(output, "%d %d\n", count, element);
               //Update indices for next access
               do {
                       ra--;
                       ca++;
                       if (ra<0) {
                              ra=MAX RINDEX-1;
                              ca=ca+(MAX_RINDEX-1);
                       ca=ca%MAX_CINDEX;
                      element = ra * MAX_CINDEX+ca;
               } while (element >= MAX_ELEMENT);
```



S-type interleaver generatior

```
program int(input,output);
{This program generates mod-k S-random and symmetric mod-k S-random interleavers.
const Nmax = 65536; {maximum interleaver size}
var G,H,I,J,K,L,M,N,S,count,temp,prt,i_,j_,k_,im,jm:longint;
    inta, hat, deint:array[0..Nmax] of longint;
    pass, good:boolean;
    s1,s2:longint; {seeds for function uniform}
    into, deinto: text;
    sym:char;
function max(x,y:longint):longint;
{Finds the maximum of x and y}
begin{max}
  if x > y
    then max := x
    else max := y;
end; {max}
function min(x,y:longint):longint;
{Finds the maximum of x and y}
begin{min}
 if x < y
    then min := x
    else min := y;
end; {min}
function uniform(var s1,s2:longint):double;
{Generates a random number from 0.0 < x < 1.0}
const m0 = 2147483562;
      m1 = 2147483563;
      m2 = 2147483399;
      a1 = 40014;
      a2 = 40692;
      q1 = 53668;
      q2 = 52774;
      r1 = 12211;
      r2 = 3791;
var k:longint;
begin{uniform}
  k := s1 div q1;
  s1 := a1*(s1-k*q1) - k*r1;
 if s1 < 0 then s1 := s1+m1;
 k := s2 div q2;
 s2 := a2*(s2-k*q2) - k*r2;
 if s2 < 0 then s2 := s2+m2;
 k := s1-s2;
 if k < 1 then k := k+m0;
 uniform := k/m1;
end; {uniform}
procedure srandom;
{Generates mod-k S-random interleaver}
label 98;
procedure reject;
{reject random number}
begin{reject}
 count := count-1;
 if count = 0
    then begin{bad int}
           good := false;
           goto 98;
         end; {bad int}
```



```
pass := false;
  for M := K to count-1 do
    hat[M] := hat[M+1];
  hat[count] := J;
end; {reject}
begin{S-random}
  repeat
    writeln('seed1 = ',s1:1,', seed2 = ',s2:1);
    good := true;
    for I := 0 to N-1 do
      hat[I] := I;
    for I := 0 to N-1 do
      begin{make int}
        count := N-I;
        i_ := I mod k_;
        im := min(i_,k_-i_);
        repeat
          pass := true;
          K := trunc(count*uniform(s1,s2));
          if K = count then K := K-1;
          J := hat[K];
          if k > 1 then
            begin{mod k test}
              j_ := J mod k_;
              jm := min(j_, k_-j_);
              if im <> jm then reject;
            end; {mod k test}
          if pass = true then
            begin(S-random test)
              for L := max(0,I-S) to I-1 do
                if (abs(J-inta[L]) <= S) and (pass = true) then reject;
            end(S-random test)
        until pass = true;
        for M := K to N-I-2 do
          hat[M] := hat[M+1];
        inta[I] := J;
      end; {make int}
    98:
  until good = true;
end{S-random};
procedure trandom;
{Generates symmetric mod-k S-random interleaver}
label 99;
procedure rejectS;
{reject random number}
begin{reject S}
  count := count-1;
  if count = 0 then
    begin{bad int}
      good := false;
      goto 99;
    end; {bad int}
  pass := false;
  inta[I] := -1;
  inta[J] := -1;
  for M := K to count-1 do
   hat[M] := hat[M+1];
  hat[count] := J;
end; {reject S}
procedure test;
{S-random test}
begin{test}
  if (inta[L] >= 0) and (abs(G-inta[L]) <= S) then rejectS;</pre>
  L := L+1;
end; {test}
begin {T-random}
```



```
repeat
    writeln('seed1 = ',s1:1,', seed2 = ',s2:1);
    good := true;
    for I := 0 to N-1 do
     begin{init}
        hat[I] := I;
        inta[I] := -1;
      end; {init}
    H := N;
    I := 0;
    repeat
     count := H;
     while (inta[I] \geq= 0) and (I < N) do I := I+1;
     i_ := I mod k_;
     im := min(i_,k_-i_);
     repeat
        pass := true;
        K := trunc(count*uniform(s1,s2));
        if K = count then K := K-1;
        J := hat[K];
        if k_{-} > 1 then
          begin{mod k test}
            j_ := J mod k_;
            jm := min(j_,k_-j_);
            if im <> jm then rejectS;
          end; {mod k test}
        if pass = true then
          begin{S-random test}
            inta[I] := J;
            inta[J] := I;
            G := J;
            L := max(0, I-S);
            while (pass = true) and (L < I) do test;
            L := I+1;
            while (pass = true) and (L < min(I+S,N)) do test;
            G := I;
            L := max(0, J-S);
            while (pass = true) and (L < J) do test;
            L := J+1;
           while (pass = true) and (L < min(J+S,N)) do test;
          end; {S-random test}
     until pass = true;
      H := H-1;
      for M := K to H-1 do
        hat[M] := hat[M+1];
      if I <> J then
        begin{sym}
        · K := 0;
          while (hat[K] \iff I) and (K \iff H) do K := K+1;
          H := H-1;
          for M := K to H-1 do
           hat[M] := hat[M+1];
        end; {sym}
    until H = 0;
    99:
 until good = true;
end{T-random};
 s1 := 12345; {initialise seeds for uniform}
 s2 := 67890;
 writeln('Random Interleaver Generator V1.01');
 writeln('Copyright (c) 1998 Small World Communications. All rights reserved.');
 writeln;
 write('Enter block size N <= ',Nmax:1,': ');</pre>
 readln(N);
 write('Enter S parameter (S=1 is random): ');
readln(S);
```



```
write('Enter mod-k parameter (k=1 is normal): ');
readln(k_);
repeat
  write('Do you want a symmetric interleaver? ');
  readln(sym);
  pass := (sym = 'y') or (sym = 'Y') or (sym = 'n') or (sym = 'N');
  if pass = false then
    writeln('Invalid entry. Try again.');
until pass = true;
writeln;
{\tt case \; sym \; of }
  'y', 'Y': trandom; 'n', 'N': srandom;
end; {case}
assign(into,'int.dat');
rewrite(into);
for I := 0 to N-1 do
  writeln(into,inta[I]:1);
close(into);
for I := 0 to N-1 do
  hat[I] := 0;
for I := 0 to N-1 do
  begin{test}
    J := inta[I];
    hat[J] := hat[J] + 1;
  end; {test}
pass := true;
for I := 0 to N-1 do
  if hat[I] < 1 then pass := false;</pre>
if pass = false
  then writeln('Bad interleaver!');
pass := true;
I := 0;
repeat
  J := inta[I];
  for L := max(0, I-S) to I-1 do
    if (abs(J-inta[L]) \le S) and (pass = true)
      then begin
              pass := false;
              writeln('Interleaver failed S-test');
writeln(I:1,' ',inta[I]:1,' ',L:1,' ',inta[L]:1);
            end;
  I := I+1:
until (pass = false) or (I = N);
K := 0;
for I := 0 to N-1 do
 K := max(K, abs(I-inta[I]));
writeln('Dmin = ',K:1);
writeln('Interleaver table int.dat succussfully generated');
```